“Dear Sir: You say that \( x^3 \) is called \( x \)-cubed.”

“And you say that \( x^2 \) is called \( x \)-squared.”

“So, why isn’t \( x^1 \) called \( x \)-lined?”

“Don’t expect an answer to this one.

“See, it’s working.”

“My sign on adding fractions with unlike denominators is keeping the hyenas away.”

There aren’t any hyenas around here.

\[ \frac{1}{2} + \frac{1}{3} = \frac{3}{6} + \frac{2}{6} = \frac{5}{6} \]

\[ \frac{1}{2} + \frac{1}{3} = \frac{3}{6} + \frac{2}{6} = \frac{5}{6} \]
What You Learned Before

Identifying Prime and Composite Numbers

Example 1 Determine whether 26 is prime or composite. Because the factors of 26 are 1, 2, 13, and 26, it is composite.

Example 2 Determine whether 37 is prime or composite. Because the only factors of 37 are 1 and 37, it is prime.

Try It Yourself

Determine whether the number is prime or composite.

1. 5  
2. 14  
3. 17  
4. 23  
5. 28  
6. 33  
7. 43  
8. 57  
9. 64

Adding and Subtracting Mixed Numbers with Like Denominators

Example 3 Find \( \frac{3}{5} + \frac{1}{5} \)

\[
\frac{3}{5} + \frac{1}{5} = \frac{2 \cdot 5 + 3}{5} + \frac{4 \cdot 5 + 1}{5}
\]

Rewrite the mixed numbers as improper fractions.

\[
= \frac{13}{5} + \frac{21}{5}
\]

Simplify.

\[
= \frac{13 + 21}{5}
\]

Add the numerators.

\[
= \frac{34}{5}, \text{ or } 6 \frac{4}{5}
\]

Simplify.

Try It Yourself

Add or subtract.

10. \( \frac{4}{9} + \frac{7}{9} \)  
11. \( \frac{6}{11} + \frac{3}{11} \)  
12. \( \frac{7}{8} + \frac{3}{8} \)

13. \( \frac{8}{13} - \frac{2}{13} \)  
14. \( \frac{1}{4} - \frac{3}{4} \)  
15. \( \frac{1}{6} - \frac{5}{6} \)
1.1 Whole Number Operations

Essential Question: How do you know which operation to choose when solving a real-life problem?

ACTIVITY: Choosing an Operation

Work with a partner. The double bar graph shows the history of a citywide cleanup day.

- Copy each question below.
- Underline a key word or phrase that helps you know which operation to use to answer the question. State the operation. Why do you think the key word or phrase indicates the operation you chose?
- Write an expression you can use to answer the question.
- Find the value of your expression.

a. What is the total amount of trash collected from 2010 to 2013?

b. How many more pounds of recyclables were collected in 2013 than in 2010?

c. How many times more recyclables were collected in 2012 than in 2010?

d. The amount of trash collected in 2014 is estimated to be twice the amount collected in 2011. What is that amount?
Work with a partner.

a. Explain how you can use estimation to check the reasonableness of the value of your expression in Activity 1(a).

b. Explain how you can use addition to check the value of your expression in Activity 1(b).

c. Explain how you can use estimation to check the reasonableness of the value of your expression in Activity 1(c).

d. Use mental math to check the value of your expression in Activity 1(d). Describe your strategy.

Work with a partner. Use the map. Explain how you found each answer.

a. Which two lakes have a combined area of about 33,000 square miles?

b. Which lake covers an area about three times greater than the area of Lake Erie?

c. Which lake covers an area that is about 16,000 square miles greater than the area of Lake Ontario?

d. Estimate the total area covered by the Great Lakes.

What Is Your Answer?

4. IN YOUR OWN WORDS How do you know which operation to choose when solving a real-life problem?

5. In a magic square, the sum of the numbers in each row, column, and diagonal is the same and each number from 1 to 9 is used only once. Complete the magic square. Explain how you found the missing numbers.

Use what you learned about choosing operations to complete Exercises 8–11 on page 7.
Recall the four basic operations: addition, subtraction, multiplication, and division.

<table>
<thead>
<tr>
<th>Operation</th>
<th>Words</th>
<th>Algebra</th>
</tr>
</thead>
<tbody>
<tr>
<td>Addition</td>
<td>the sum of</td>
<td>$a + b$</td>
</tr>
<tr>
<td>Subtraction</td>
<td>the difference of</td>
<td>$a - b$</td>
</tr>
<tr>
<td>Multiplication</td>
<td>the product of</td>
<td>$a \times b$</td>
</tr>
<tr>
<td>Division</td>
<td>the quotient of</td>
<td>$\frac{a}{b}$</td>
</tr>
</tbody>
</table>

### Example 1: Adding and Subtracting Whole Numbers

The bar graph shows the attendance at a three-day art festival.

**a. What is the total attendance for the art festival?**

You want to find the total attendance for the three days. In this case, the phrase *total attendance* indicates you need to find the sum of the daily attendances.

Line up the numbers by their place values, then add.

The total attendance is 9591 people.

**b. What is the increase in attendance from Day 1 to Day 2?**

You want to find how many more people attended on Day 2 than on Day 1. In this case, the phrase *how many more* indicates you need to find the difference of the attendances on Day 2 and Day 1.

Line up the numbers by their place values, then subtract.

The increase in attendance from Day 1 to Day 2 is 575 people.

### Example 2: Multiplying Whole Numbers

A school lunch contains 12 chicken nuggets. Ninety-five students buy the lunch. What is the total number of chicken nuggets served?

You want to find the total number of chicken nuggets in 95 groups of 12 chicken nuggets. The phrase *95 groups of 12* indicates you need to find the product of 95 and 12.

\[
12 \times 95 = 1140
\]

Because 1200 \approx 1140, the answer is reasonable.

There were 1140 chicken nuggets served.
Section 1.1  Whole Number Operations  

**On Your Own**  

Find the value of the expression. Use estimation to check your answer.  

1. 1745 + 682  
2. 912 − 799  
3. 42 × 118  

---  

**EXAMPLE**  

**Dividing Whole Numbers: No Remainder**  

You make 24 equal payments for a go-kart. You pay a total of $840. How much is each payment?  

You want to find the number of groups of 24 in $840. The phrase *groups of 24 in $840* indicates you need to find the quotient of 840 and 24.  

Use long division to find the quotient.  

Decide where to write the first digit of the quotient.  

\[
\begin{array}{c|cc}
\text{24} & \text{840} \\
\hline
\text{24} & \text{840} \\
\text{− 72} & \text{0} \\
\text{12} & \text{0} \\
\end{array}
\]

Do not use the hundreds place because 24 is greater than 8.  

Use the tens place because 24 is less than 84.  

So, divide the tens and write the first digit of the quotient in the tens place.  

\[
\begin{array}{c|cc}
\text{24} & \text{840} \\
\hline
\text{24} & \text{840} \\
\text{− 72} & \text{120} \\
\text{12} & \text{0} \\
\end{array}
\]

Divide 84 by 24: There are three groups of 24 in 84.  

Multiply 3 and 24.  

Subtract 72 from 84.  

Next, bring down the 0 and divide the ones.  

\[
\begin{array}{c|cc}
\text{24} & \text{840} \\
\hline
\text{24} & \text{840} \\
\text{− 72} & \text{120} \\
\text{12} & \text{0} \\
\end{array}
\]

Divide 120 by 24: There are five groups of 24 in 120.  

Multiply 5 and 24.  

Subtract 120 from 120.  

The quotient of 840 and 24 is 35.  

So, each payment is $35.  

---  

**Remember**  

\[
\frac{\text{dividend}}{\text{divisor}} = \text{quotient} \\
\text{So, quotient} \times \text{divisor} = \text{dividend.}
\]

**Check**  

Find the product of the quotient and the divisor.  

\[
\begin{array}{c|c}
\text{quotient} & \text{divisor} \\
\hline
35 & 24 \\
140 & 70 \\
840 & \checkmark
\end{array}
\]
Chapter 1  Numerical Expressions and Factors

Find the value of the expression. Use estimation to check your answer.

4. $234 \div 9$
5. $\frac{986}{58}$
6. $840 \div 105$

7. Find the quotient of 9920 and 320.

When you use long division to divide whole numbers and you obtain a remainder, you can write the quotient as a mixed number using the rule

\[
\text{dividend} \div \text{divisor} = \text{quotient} + \frac{\text{remainder}}{\text{divisor}}.
\]

**EXAMPLE 4**

**Real-Life Application**

A 301-foot-high swing at an amusement park can take 64 people on each ride. A total of 8983 people ride the swing today. All the rides are full except for the last ride. How many rides are given? How many people are on the last ride?

To find the number of rides given, you need to find the number of groups of 64 people in 8983 people. The phrase "groups of 64 people in 8983 people" indicates you need to find the quotient of 8983 and 64.

Divide the place-value positions from left to right.

\[
\begin{array}{c|c|c}
64 & 8983 \\
\hline
& 140 R23 \\
\hline
64 & 8983 \\
\hline
64 & \underline{64} \\
\hline
& 258 \\
\hline
64 & \underline{256} \\
\hline
& 23 \\
\hline
64 & \underline{0} \\
\hline
& 23 \\
\end{array}
\]

There is one group of 64 in 89.

There are four groups of 64 in 258.

There are no groups of 64 in 23.

The remainder is 23.

The quotient is $140\frac{23}{64}$. This indicates 140 groups of 64, with 23 remaining.

So, 141 rides are given, with 23 people on the last ride.

**On Your Own**

Find the value of the expression. Use estimation to check your answer.

8. $\frac{6096}{30}$
9. $45,691 \div 28$
10. $3215 \div 430$

11. **WHAT IF?** In Example 4, 9038 people ride the swing. What is the least number of rides possible?
1.1 Exercises

Vocabulary and Concept Check:

VOCABULARY Determine which operation the word or phrase represents.

1. sum
2. times
3. the quotient of
4. decreased by
5. total of
6. minus

7. VOCABULARY Use the division problem shown to tell whether the number is the divisor, dividend, or quotient.
   a. 884
   b. 26
   c. 34

Practice and Problem Solving

The bar graph shows the attendance at a food festival. Write an expression you can use to answer the question. Then find the value of your expression.

8. What is the total attendance at the food festival from 2010 to 2013?
9. How many more people attended the food festival in 2012 than in 2011?
10. How many times more people attended the food festival in 2013 than in 2010?
11. The festival projects that the total attendance for 2014 will be twice the attendance in 2012. What is the projected attendance for 2014?

Find the value of the expression. Use estimation to check your answer.

12. 2219 + 872
13. 5351 + 1730
14. 3968 + 1879
15. 7694 − 5232
16. 9165 − 4729
17. 2416 − 1983
18. 84 × 37
19. 124 × 56
20. 419 × 236
21. 837 ÷ 27
22. \( \frac{588}{84} \)
23. 7440 ÷ 124
24. 6409 ÷ 61
25. 8241 ÷ 173
26. \( \frac{33,505}{160} \)

Section 1.1 Whole Number Operations
ERROR ANALYSIS  Describe and correct the error in finding the value of the expression.

27.  \[ \begin{array}{c}
39 \\
\times 17 \\
273 \\
39 \\
312 \\
\end{array} \]

Determine the operation you would use to solve the problem.  Do not answer the question.

29.  Gymnastic lessons cost $30 per week. How much will 18 weeks of gymnastic lessons cost?

30.  The scores on your first two tests were 82 and 93. By how many points did your score improve?

31.  You are setting up tables for a banquet for 150 guests. Each table seats 12 people. What is the minimum number of tables you will need?

32.  A store has 15 boxes of peaches. Each box contains 45 peaches. How many peaches does the store have?

33.  Two shirts cost $18 and $25. What is the total cost of the shirts?

34.  A gardener works for 14 hours during a week and charges $168. How much does the gardener charge for each hour?

Find the perimeter and area of the rectangle.

35.  \[ \begin{array}{c}
5 \text{ in.} \\
7 \text{ in.} \\
\end{array} \]

36.  \[ \begin{array}{c}
9 \text{ ft} \\
12 \text{ ft} \\
\end{array} \]

37.  \[ \begin{array}{c}
8 \text{ m} \\
10 \text{ m} \\
\end{array} \]

38.  BOX OFFICE  The number of tickets sold for the opening weekend of a movie is 879,575. The movie was shown in 755 theaters across the nation. What was the average number of tickets sold at each theater?

39.  LOGIC  You find that the product of 93 and 6 is 558. How can you use addition to check your answer? How can you use division to check your answer?

40.  NUMBER SENSE  Without calculating, decide which is greater: 3999 \div 129 or 3834 \div 142. Explain.
41. **REASONING** In a division problem, can the remainder be greater than the divisor? Explain.

42. **WATER COOLER** You change the water jug on the water cooler. How many cups can be completely filled before you need to change the water jug again?

43. **ARCADE** You have $9, one of your friends has $10, and two of your other friends each have $13. You combine your money to buy arcade tokens. You use a coupon to buy 8 tokens for $1. The cost of the remaining tokens is four for $1. You and your friends share the tokens evenly. How many tokens does each person get?

44. **BOOK SALE** You borrow bookcases like the one shown to display 943 books at a book sale. You plan to put 22 books on each shelf. No books will be on top of the bookcases.
   a. How many bookcases must you borrow to display all the books?
   b. You fill the shelves of each bookcase in order, starting with the top shelf. How many books are on the third shelf of the last bookcase?

45. **MODELING** The siding of a house is 2250 square feet. The siding needs two coats of paint. The table shows information about the paint.
   a. What is the minimum cost of the paint needed to complete the job?
   b. How much paint is left over?

46. **Use the digits 3, 4, 6, and 9 to complete the division problem. Use each digit once.**

<table>
<thead>
<tr>
<th>Can Size</th>
<th>Cost</th>
<th>Coverage</th>
</tr>
</thead>
<tbody>
<tr>
<td>1 quart</td>
<td>$18</td>
<td>80 square feet</td>
</tr>
<tr>
<td>1 gallon</td>
<td>$29</td>
<td>320 square feet</td>
</tr>
</tbody>
</table>

47. **Plot the ordered pair in a coordinate plane.**

48. **(1, 3)**

49. **(0, 4)**

50. **(6, 0)**

51. **MULTIPLE CHOICE** Which of the following numbers is **not** prime?

   - **A** 1
   - **B** 2
   - **C** 3
   - **D** 5

Section 1.1 Whole Number Operations
1.2 Powers and Exponents

Essential Question  How can you use repeated factors in real-life situations?

As I was going to St. Ives
I met a man with seven wives
Each wife had seven sacks
Each sack had seven cats
Each cat had seven kits
Kits, cats, sacks, wives
How many were going to St. Ives?  Nursery Rhyme, 1730

ACTIVITY: Analyzing a Math Poem

Work with a partner. Here is a “St. Ives” poem written by two students. Answer the question in the poem.

As I was walking into town
I met a ringmaster with five clowns
Each clown had five magicians
Each magician had five bunnies
Each bunny had five fleas
Fleas, bunnies, magicians, clowns
How many were going into town?

Numerical Expressions

In this lesson, you will
• write expressions as powers.
• find values of powers.

Number of clowns:  5
Number of magicians:  5 \times 5
Number of bunnies:  5 \times 5 \times 5
Number of fleas:  5 \times 5 \times 5 \times 5

So, the number of fleas, bunnies, magicians, and clowns is \text{________}. Explain how you found your answer.
**2 ACTIVITY: Writing Repeated Factors**

Work with a partner. Copy and complete the table.

<table>
<thead>
<tr>
<th>Repeated Factors</th>
<th>Using an Exponent</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>a. $4 \times 4$</td>
<td></td>
<td></td>
</tr>
<tr>
<td>b. $6 \times 6$</td>
<td></td>
<td></td>
</tr>
<tr>
<td>c. $10 \times 10 \times 10$</td>
<td></td>
<td></td>
</tr>
<tr>
<td>d. $100 \times 100 \times 100$</td>
<td></td>
<td></td>
</tr>
<tr>
<td>e. $3 \times 3 \times 3$</td>
<td></td>
<td></td>
</tr>
<tr>
<td>f. $4 \times 4 \times 4 \times 4$</td>
<td></td>
<td></td>
</tr>
<tr>
<td>g. $2 \times 2 \times 2 \times 2 \times 2$</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

h. In your own words, describe what the two numbers in the expression $3^5$ mean.

**3 ACTIVITY: Writing and Analyzing a Math Poem**

Work with a partner.

a. Write your own “St. Ives” poem.

b. Draw pictures for your poem.

c. Answer the question in your poem.

d. Show how you can use exponents to write your answer.

**What Is Your Answer?**

4. **IN YOUR OWN WORDS** How can you use repeated factors in real-life situations? Give an example.

5. **STRUCTURE** Use exponents to complete the table. Describe the pattern.

<p>| | | | | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>10</td>
<td>100</td>
<td>1000</td>
<td>10,000</td>
<td>100,000</td>
</tr>
<tr>
<td>$10^1$</td>
<td>$10^2$</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Practice

Use what you learned about exponents to complete Exercises 4–6 on page 14.

Section 1.2 Powers and Exponents 11
A **power** is a product of repeated factors. The **base** of a power is the repeated factor. The **exponent** of a power indicates the number of times the base is used as a factor.

\[ 3^4 = 3 \cdot 3 \cdot 3 \cdot 3 \]

**power** \(3\) is used as a factor 4 times.

<table>
<thead>
<tr>
<th>Power</th>
<th>Words</th>
</tr>
</thead>
<tbody>
<tr>
<td>(3^2)</td>
<td>Three squared, or three to the second</td>
</tr>
<tr>
<td>(3^3)</td>
<td>Three cubed, or three to the third</td>
</tr>
<tr>
<td>(3^4)</td>
<td>Three to the fourth</td>
</tr>
</tbody>
</table>

**EXAMPLE** 1 **Writing Expressions as Powers**

Write each product as a power.

a. \(4 \times 4 \times 4 \times 4 \times 4\)

Because 4 is used as a factor 5 times, its exponent is 5.

\[4 \times 4 \times 4 \times 4 \times 4 = 4^5.\]

\[\because\] So, \(4 \times 4 \times 4 \times 4 \times 4 = 4^5.\)

b. \(12 \times 12 \times 12\)

Because 12 is used as a factor 3 times, its exponent is 3.

\[\because\] So, \(12 \times 12 \times 12 = 12^3.\)

**On Your Own**

Write the product as a power.

1. \(6 \times 6 \times 6 \times 6 \times 6\)
2. \(15 \times 15 \times 15 \times 15\)

**EXAMPLE** 2 **Finding Values of Powers**

Find the value of each power.

a. \(7^2\)

\[7^2 = 7 \times 7\]

\[= 49\]

Write as repeated multiplication. Simplify.

b. \(5^3\)

\[5^3 = 5 \times 5 \times 5\]

\[= 125\]
The square of a whole number is a **perfect square**.

### EXAMPLE 3  Identifying Perfect Squares

Determine whether each number is a perfect square.

**a.** $64$

Because $8^2 = 64$, $64$ is a perfect square.

**b.** $20$

No whole number squared equals $20$. So, $20$ is not a perfect square.

### On Your Own

Find the value of the power.

**3.** $6^3$

**4.** $9^2$

**5.** $3^4$

**6.** $18^2$

Determine whether the number is a perfect square.

**7.** $25$

**8.** $2$

**9.** $99$

**10.** $100$

### Remember

The area of a square is equal to its side length squared.

$$\text{Area} = s^2$$

The area of the square traffic sign is $3^2 = 9$ square units.

### EXAMPLE 4  Real-Life Application

A MONOPOLY® game board is a square with a side length of $20$ inches. What is the area of the game board?

Use a verbal model to solve the problem.

area of game board $= (\text{side length})^2$

$= 20^2$ Substitute $20$ for side length.

$= 400$ Multiply.

The area of the game board is $400$ square inches.

### On Your Own

11. What is the area of the square traffic sign in square inches? in square feet?
1.2 Exercises

Vocabulary and Concept Check

1. **VOCABULARY** How are exponents and powers different?

2. **VOCABULARY** Is 10 a perfect square? Is 100 a perfect square? Explain.

3. **WHICH ONE DOESN'T BELONG?** Which one does not belong with the other three? Explain your reasoning.

   \[2^4 = 2 \times 2 \times 2 \times 2\]  
   \[3 + 3 + 3 + 3 = 3(4)\]  
   \[3^2 = 3 \times 3\]  
   \[5 \times 5 \times 5 = 5^3\]

Practice and Problem Solving

Write the product as a power.

4. \[9 \times 9\]

5. \[13 \times 13\]

6. \[15 \times 15 \times 15\]

7. \[2 \times 2 \times 2 \times 2 \times 2\]

8. \[14 \times 14 \times 14\]

9. \[8 \times 8 \times 8 \times 8\]

10. \[11 \times 11 \times 11 \times 11 \times 11\]

11. \[7 \times 7 \times 7 \times 7 \times 7\]

12. \[16 \times 16 \times 16 \times 16\]

13. **ERROR ANALYSIS** Describe and correct the error in writing the product as a power.

   \[4 \times 4 \times 4 = 3^4\]

Find the value of the power.

14. \[5^2\]

15. \[4^3\]

16. \[2^5\]

17. \[14^2\]

18. \[7^6\]

19. \[4^8\]

20. \[12^4\]

21. \[17^5\]

Use a calculator to find the value of the power.

22. **ERROR ANALYSIS** Describe and correct the error in finding the value of the power.

   \[8^3 = 8 \times 3 = 24\]

23. **POPULATION** The population of Virginia is about \(8 \times 10^6\). About how many people live in Virginia?

24. **FIGURINES** The smallest figurine in a gift shop is 2 inches tall. The height of each figurine is twice the height of the previous figurine. Write a power to represent the height of the tallest figurine. Then find the height.
Determine whether the number is a perfect square.

25. 8 26. 4 27. 81 28. 44
29. 49 30. 125 31. 150 32. 144

33. **PAINTING** A square painting measures 2 meters on each side. What is the area of the painting in square centimeters?

34. **NUMBER SENSE** Write three powers that have values greater than 120 and less than 130.

35. **CHECKERS** A checkers board has 64 squares. How many squares are in each row?

36. **PATIO** A landscaper has 125 tiles to build a square patio. The patio must have an area of at least 80 square feet.
   a. What are the possible arrangements for the patio?
   b. How many tiles are not used in each arrangement?

37. **PATTERNs** Copy and complete the table. Describe what happens to the value of the power as the exponent decreases. Use this pattern to find the value of $4^0$.

<table>
<thead>
<tr>
<th>Power</th>
<th>4⁰</th>
<th>4¹</th>
<th>4²</th>
<th>4³</th>
<th>4⁴</th>
</tr>
</thead>
<tbody>
<tr>
<td>Value</td>
<td>1</td>
<td>4</td>
<td>16</td>
<td>64</td>
<td>256</td>
</tr>
</tbody>
</table>

38. **REASONING** Consider the equation $56 = \_\_^2$. The missing number is between what two whole numbers?

39. **Repeated Reasoning** How many blocks do you need to add to Square 6 to get Square 7? to Square 9 to get Square 10? to Square 19 to get Square 20? Explain.

---

**Fair Game Review** What you learned in previous grades & lessons

Find the value of the expression. *(Skills Review Handbook)*

40. $6 \times 14$ 41. $11 \times 15$ 42. $56 \div 7$ 43. $112 \div 16$

44. **MULTIPLE CHOICE** You buy a box of gum that has 12 packs. Each pack has 5 pieces. Which expression represents the total number of pieces of gum? *(Skills Review Handbook)*

A 12 + 5  B 12 − 5  C 12 × 5  D 12 ÷ 5

Section 1.2 Powers and Exponents
## Essential Question
What is the effect of inserting parentheses into a numerical expression?

### 1.3 Order of Operations

#### ACTIVITY: Comparing Different Orders

Work with a partner. Find the value of the expression by using different orders of operations. Are your answers the same? (Circle yes or no.)

<table>
<thead>
<tr>
<th>Expression</th>
<th>Order of Operations</th>
<th>Same?</th>
</tr>
</thead>
<tbody>
<tr>
<td>a. (3 + 4 \times 2 = )</td>
<td>Add, then multiply. Multiply, then add.</td>
<td>Yes No</td>
</tr>
<tr>
<td>b. (5 + 3 - 1 = )</td>
<td>Add, then subtract. Subtract, then add.</td>
<td>Yes No</td>
</tr>
<tr>
<td>c. (12 ÷ 3 \times 2 = )</td>
<td>Divide, then multiply. Multiply, then divide.</td>
<td>Yes No</td>
</tr>
<tr>
<td>d. (16 ÷ 4 + 4 = )</td>
<td>Divide, then add. Add, then divide.</td>
<td>Yes No</td>
</tr>
<tr>
<td>e. (8 \times 4 - 2 = )</td>
<td>Multiply, then subtract. Subtract, then multiply.</td>
<td>Yes No</td>
</tr>
<tr>
<td>f. (8 \times 4 ÷ 2 = )</td>
<td>Multiply, then divide. Divide, then multiply.</td>
<td>Yes No</td>
</tr>
<tr>
<td>g. (13 - 4 + 6 = )</td>
<td>Subtract, then add. Add, then subtract.</td>
<td>Yes No</td>
</tr>
<tr>
<td>h. (1 \times 2 + 3 = )</td>
<td>Multiply, then add. Add, then multiply.</td>
<td>Yes No</td>
</tr>
</tbody>
</table>

### Numerical Expressions

In this lesson, you will
- evaluate numerical expressions with whole-number exponents.
Section 1.3  
Order of Operations  
17

ACTIVITY: Using Parentheses

Work with a partner. Use all the symbols and numbers to write an expression that has the given value.

<table>
<thead>
<tr>
<th>Symbols and Numbers</th>
<th>Value</th>
<th>Expression</th>
</tr>
</thead>
<tbody>
<tr>
<td>a. ( ), +, ÷, 3, 4, 5</td>
<td>3</td>
<td></td>
</tr>
<tr>
<td>b. ( ), −, ×, 2, 5, 8</td>
<td>11</td>
<td></td>
</tr>
<tr>
<td>c. ( ), ×, ÷, 4, 4, 16</td>
<td>16</td>
<td></td>
</tr>
<tr>
<td>d. ( ), −, ÷, 3, 8, 11</td>
<td>1</td>
<td></td>
</tr>
<tr>
<td>e. ( ), +, ×, 2, 5, 10</td>
<td>70</td>
<td></td>
</tr>
</tbody>
</table>

ACTIVITY: Reviewing Fractions and Decimals

Work with a partner. Evaluate the expression.

a. \( \frac{3}{4} - \left( \frac{1}{4} + \frac{1}{2} \right) \) = 

b. \( \frac{5}{6} - \frac{1}{6} - \frac{1}{12} \) = 

c. \( 7.4 - (3.5 - 3.1) \) = 

d. \( 10.4 - (8.6 + 0.9) \) = 

e. \( ($7.23 + $2.32) - $5.40 \) = 

What Is Your Answer?

4. In an expression with two or more operations, why is it necessary to agree on an order of operations? Give examples to support your explanation.

5. **IN YOUR OWN WORDS** What is the effect of inserting parentheses into a numerical expression?

Use what you learned about the order of operations to complete Exercises 3–5 on page 20.
A **numerical expression** is an expression that contains only numbers and operations. To **evaluate**, or find the value of, a numerical expression, use a set of rules called the **order of operations**.

### Key Idea

**Order of Operations**

1. Perform operations in **P**arentheses.
2. Evaluate numbers with **E**xponents.
3. **M**ultiply or **D**ivide from left to right.
4. **A**dd or **S**ubtract from left to right.

### Example 1 Using Order of Operations

a. Evaluate \(12 - 2 \times 4\).

\[
12 - 2 \times 4 = 12 - 8 = 4
\]

Multiply 2 and 4.
Subtract 8 from 12.

b. Evaluate \(7 + 60 \div (3 \times 5)\).

\[
7 + 60 \div (3 \times 5) = 7 + 60 \div 15 = 7 + 4 = 11
\]

Perform operation in parentheses.
Divide 60 by 15.
Add 7 and 4.

### Example 2 Using Order of Operations with Exponents

Evaluate \(30 \div (7 + 2^3) \times 6\).

Evaluate the power in parentheses first.

\[
30 \div (7 + 2^3) \times 6 = 30 \div (7 + 8) \times 6 = 30 \div 15 \times 6 = 2 \times 6 = 12
\]

Evaluate \(2^3\).
Perform operation in parentheses.
Divide 30 by 15.
Multiply 2 and 6.

### On Your Own

Evaluate the expression.

1. \(7 \cdot 5 + 3\)
2. \((28 - 20) \div 4\)
3. \(6 \times 15 - 10 \div 2\)
4. \(6 + 2^4 - 1\)
5. \(4 \cdot 3^2 + 18 - 9\)
6. \(16 + (5^2 - 7) \div 3\)
The symbols $\times$ and $\cdot$ are used to indicate multiplication. You can also use parentheses to indicate multiplication. For example, $3(2 + 7)$ is the same as $3 \times (2 + 7)$.

**EXAMPLE 3** Using Order of Operations

a. Evaluate $9 + 7(5 - 2)$.

\[
9 + 7(5 - 2) = 9 + 7(3) \quad \text{Perform operation in parentheses.}
\]
\[
= 9 + 21 \quad \text{Multiply 7 and 3.}
\]
\[
= 30 \quad \text{Add 9 and 21.}
\]

b. Evaluate $15 - 4(6 + 1) \div 2^2$.

\[
15 - 4(6 + 1) \div 2^2 = 15 - 4(7) \div 4 \quad \text{Perform operation in parentheses.}
\]
\[
= 15 - 4(7) \div 4 \quad \text{Evaluate } 2^2.
\]
\[
= 15 - 28 \div 4 \quad \text{Multiply 4 and 7.}
\]
\[
= 15 - 7 \quad \text{Divide 28 by 4.}
\]
\[
= 8 \quad \text{Subtract 7 from 15.}
\]

**EXAMPLE 4** Real-Life Application

You buy foam spheres, paint bottles, and wooden rods to construct a model of our solar system. What is your total cost?

Use a verbal model to solve the problem.

\[
\text{cost of 9 spheres} + \text{cost of 6 paint bottles} + \text{cost of 8 rods}
\]
\[
9 \cdot 2 + 6 \cdot 3 + 8 \cdot 1 = 18 + 18 + 8 \quad \text{Multiply.}
\]
\[
= 44 \quad \text{Add.}
\]

Your total cost is $44.

**On Your Own**

Evaluate the expression.

7. $50 + 6(12 \div 4) - 8^2$

8. $5^2 - 5(10 - 5)$

9. $\frac{8(3 + 4)}{7}$

10. **WHAT IF?** In Example 4, you add the dwarf planet Pluto to your model. Use a verbal model to find your total cost assuming you do not need more paint. Explain.
1.3 Exercises

Vocabulary and Concept Check

1. WRITING Why does 12 − 8 ÷ 2 = 8, but (12 − 8) ÷ 2 = 2?
2. REASONING Describe the steps in evaluating the expression 8 ÷ (6 − 4) + 3².

Practice and Problem Solving

Find the value of the expression.
3. (4 × 15) − 3
4. 10 − (7 + 1)
5. 18 ÷ (6 + 3)

Evaluate the expression.

6. 5 + 18 ÷ 6
7. (11 − 3) ÷ 2 + 1
8. 45 ÷ 9 × 12
9. 6² − 3 • 4
10. 42 ÷ (15 − 2³)
11. 4² • 2 + 8 • 7
12. 3² + 12 ÷ (6 − 3) × 8
13. (10 + 4) ÷ (26 − 19)
14. (5² − 4) • 2 − 18

ERROR ANALYSIS Describe and correct the error in evaluating the expression.

15. \[9 + 2 \times 3 = 11 \times 3 = 33\]
16. \[19 − 6 + 12 = 19 − 18 = 1\]

17. POETRY You need to read 20 poems in 5 days for an English project. Each poem is 2 pages long. Evaluate the expression 20 × 2 ÷ 5 to find how many pages you need to read each day.

Evaluate the expression.

18. 9² − 8(6 + 2)
19. (3 − 1)³ + 7(6) − 5²
20. 8\left(\frac{1}{6} + \frac{5}{6}\right) ÷ 4
21. 7² − 2\left(\frac{11}{8} − \frac{3}{8}\right)
22. 8(7.3 + 3.7) − 14 ÷ 2
23. 2⁴(5.2 − 3.2) ÷ 4

24. MONEY You have four $10 bills and eighteen $5 bills in your piggy bank. How much money do you have?

25. THEATER Before a show, there are 8 people in a theater. Five groups of 4 people enter, and then three groups of 2 people leave. Evaluate the expression 8 + 5(4) − 3(2) to find how many people are in the theater.

Evaluate the expression.

\[4(\$10) + 18(\$5)\]
Evaluate the expression.

26. $\frac{6(3 + 5)}{4}$
27. $\frac{12^2 - 4(6) + 1}{11^2}$
28. $\frac{26 \div 2 + 5}{3^2 - 3}$

29. **FIELD TRIP** Eighty students are going on a field trip to a history museum. The total cost includes
   - 2 bus rentals and
   - $10 per student for lunch.
What is the total cost per student?

30. **OPEN-ENDED** Use all four operations without parentheses to write an expression that has a value of 100.

31. **SHOPPING** You buy 6 notebooks, 10 folders, 1 pack of pencils, and 1 lunch box for school. After using a $10 gift card, how much do you owe? Explain how you solved the problem.

32. **LITTER CLEANUP** Two groups collect litter along the side of a road. It takes each group 5 minutes to clean up a 200-yard section. How long does it take to clean up 2 miles? Explain how you solved the problem.

33. **Number Sense** Copy each statement. Insert $+, - \times$, or $\div$ symbols to make each statement true.
   - a. $27 \underline{3} \underline{5} 2 = 19$
   - b. $9^2 \underline{11} \underline{8} 4 \underline{1} = 60$
   - c. $5 \underline{6} \underline{15} 9 = 24$
   - d. $14 \underline{2} \underline{7} 3 \underline{9} = 10$

34. **Add or subtract**. *(Skills Review Handbook)*
   - 34. $5.2 + 0.5$
   - 35. $8 - 1.9$
   - 36. $12.6 - 3$
   - 37. $0.7 + 0.2$

38. **MULTIPLE CHOICE** You are making two recipes. One recipe calls for $2\frac{1}{3}$ cups of flour. The other recipe calls for $1\frac{3}{4}$ cups of flour. How much flour do you need to make both recipes? *(Skills Review Handbook)*
   - A. $1\frac{1}{12}$ cups
   - B. $3\frac{1}{12}$ cups
   - C. $3\frac{2}{7}$ cups
   - D. $3\frac{7}{12}$ cups

Section 1.3 Order of Operations 21
You can use an information frame to help you organize and remember concepts. Here is an example of an information frame for powers.

**Words:**
A power is a product of repeated factors. The base of a power is the common factor. The exponent of a power indicates the number of times the base is used as a factor.

**Example:**
Find the value of the power.
\[2^4 = 2 \cdot 2 \cdot 2 \cdot 2 = 16\]

**On Your Own**
Make information frames to help you study these topics.
1. adding whole numbers
2. subtracting whole numbers
3. multiplying whole numbers
4. dividing whole numbers
5. order of operations

After you complete this chapter, make information frames for the following topics.
6. prime factorization
7. greatest common factor (GCF)
8. least common multiple (LCM)
9. least common denominator (LCD)
### 1.1–1.3 Quiz

Find the value of the expression. Use estimation to check your answer.  *(Section 1.1)*

<p>| | |</p>
<table>
<thead>
<tr>
<th></th>
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</thead>
<tbody>
<tr>
<td>1.</td>
<td>$4265 + 3896$</td>
</tr>
<tr>
<td>2.</td>
<td>$5327 - 2624$</td>
</tr>
<tr>
<td>3.</td>
<td>$276 \times 49$</td>
</tr>
<tr>
<td>4.</td>
<td>$648 \div 72$</td>
</tr>
</tbody>
</table>

Find the value of the power.  *(Section 1.2)*

<p>| | |</p>
<table>
<thead>
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<tbody>
<tr>
<td>5.</td>
<td>$3^3$</td>
</tr>
<tr>
<td>6.</td>
<td>$11^2$</td>
</tr>
</tbody>
</table>

Determine whether the number is a perfect square.  *(Section 1.2)*

<p>| | |</p>
<table>
<thead>
<tr>
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<tbody>
<tr>
<td>7.</td>
<td>36</td>
</tr>
<tr>
<td>8.</td>
<td>15</td>
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</tbody>
</table>

Evaluate the expression.  *(Section 1.3)*

<p>| | |</p>
<table>
<thead>
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</thead>
<tbody>
<tr>
<td>9.</td>
<td>$6 + 21 \div 7$</td>
</tr>
<tr>
<td>10.</td>
<td>$\frac{4(12 - 3)}{12}$</td>
</tr>
<tr>
<td>11.</td>
<td>$16 \div 2^3 + 6 - 2$</td>
</tr>
<tr>
<td>12.</td>
<td>$2 \times 14 \div (3^2 - 2)$</td>
</tr>
</tbody>
</table>

13. **AUDITORIUM** An auditorium has a total of 592 seats. There are 37 rows of seats, and each row has the same number of seats. How many seats are there in a single row?  *(Section 1.1)*

14. **SOFTBALL** The bases on a softball field are square. What is the area of each base?  *(Section 1.2)*

15. **DUATHLON** In an 18-mile duathlon, you run, then bike 12 miles, and then run again. The two runs are the same distance. Find the distance of each run.  *(Section 1.3)*

16. **AMUSEMENT PARK** Tickets for an amusement park cost $10 for adults and $6 for children. Find the total cost for 2 adults and 3 children.  *(Section 1.3)*
Essential Question Without dividing, how can you tell when a number is divisible by another number?

1. ACTIVITY: Finding Divisibility Rules for 2, 3, 5, and 10

Work with a partner. Copy the set of numbers (1–50) as shown.

<table>
<thead>
<tr>
<th></th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
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<tbody>
<tr>
<td></td>
<td>11</td>
<td>12</td>
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<td>41</td>
<td>42</td>
<td>43</td>
<td>44</td>
<td>45</td>
<td>46</td>
<td>47</td>
<td>48</td>
<td>49</td>
<td>50</td>
</tr>
</tbody>
</table>

a. Highlight all the numbers that are divisible by 2.
b. Put a box around the numbers that are divisible by 3.
c. Underline the numbers that are divisible by 5.
d. Circle the numbers that are divisible by 10.
e. STRUCTURE In parts (a)–(d), what patterns do you notice? Write four rules to determine when a number is divisible by 2, 3, 5, and 10.

2. ACTIVITY: Finding Divisibility Rules for 6 and 9

Work with a partner.

a. List ten numbers that are divisible by 6. Write a rule to determine when a number is divisible by 6. Use a calculator to check your rule with large numbers.
b. List ten numbers that are divisible by 9. Write a rule to determine when a number is divisible by 9. Use a calculator to check your rule with large numbers.
Work with three other students. Use the following rules and only the prime factors 2, 3, and 5 to write each number below as a product.

- Your group should have four sets of cards: a set with all 2s, a set with all 3s, a set with all 5s, and a set of blank cards. Each person gets one set of cards.
- Begin by choosing two cards to represent the given number as a product of two factors. The person with the blank cards writes any factors that are not 2, 3, or 5.
- Use the cards again to represent any number written on a blank card as a product of two factors. Continue until you have represented each handwritten card as a product of two prime factors.
- You may use only one blank card for each step.

b. 80
c. 162
d. 300

e. Compare your results with those of other groups. Are your steps the same for each number? Is your final answer the same for each number?

**What Is Your Answer?**

4. **IN YOUR OWN WORDS** Without dividing, how can you tell when a number is divisible by another number? Give examples to support your explanation.

5. Explain how you can use your divisibility rules from Activities 1 and 2 to help with Activity 3.

Use what you learned about divisibility rules to complete Exercises 4–7 on page 28.
Because 2 is a factor of 10 and \(2 \cdot 5 = 10\), 5 is also a factor of 10. The pair 2, 5 is called a \textit{factor pair} of 10.

**Example 1** Finding Factor Pairs

The brass section of a marching band has 30 members. The band director arranges the brass section in rows. Each row has the same number of members. How many possible arrangements are there?

Use the factor pairs of 30 to find the number of arrangements.

\[
\begin{align*}
30 &= 1 \cdot 30 & & \text{There could be 1 row of 30 or 30 rows of 1.} \\
30 &= 2 \cdot 15 & & \text{There could be 2 rows of 15 or 15 rows of 2.} \\
30 &= 3 \cdot 10 & & \text{There could be 3 rows of 10 or 10 rows of 3.} \\
30 &= 5 \cdot 6 & & \text{There could be 5 rows of 6 or 6 rows of 5.} \\
30 &= 6 \cdot 5 & & \text{The factors 5 and 6 are already listed.}
\end{align*}
\]

There are 8 possible arrangements: 1 row of 30, 30 rows of 1, 2 rows of 15, 15 rows of 2, 3 rows of 10, 10 rows of 3, 5 rows of 6, or 6 rows of 5.

**On Your Own**

List the factor pairs of the number.

1. 18
2. 24
3. 51

\[\text{4. WHAT IF? The woodwinds section of the marching band has 38 members. Which has more possible arrangements, the brass section or the woodwinds section? Explain.}\]

**Key Idea**

\textbf{Prime Factorization}

The \textit{prime factorization} of a composite number is the number written as a product of its prime factors.

You can use factor pairs and a \textit{factor tree} to help find the prime factorization of a number. The factor tree is complete when only prime factors appear in the product. A factor tree for 60 is shown.

\[
\begin{align*}
60 &= 2 \cdot 30 \\
60 &= 2 \cdot 2 \cdot 15 \\
60 &= 2 \cdot 2 \cdot 3 \cdot 5, \text{ or } 2^2 \cdot 3 \cdot 5
\end{align*}
\]
EXAMPLE 2 

Writing a Prime Factorization

Write the prime factorization of 48.

Choose any factor pair of 48 to begin the factor tree.

Tree 1

```
48
2 2
/  /
2 4
/  /
4 2
```

Tree 2

```
48
3 3
/  /
2 16
/  /
2 8
/  /
2 2
```

48 = 2 \cdot 2 \cdot 3 \cdot 2 \cdot 2

\[ \text{The prime factorization of 48 is } 2^4 \cdot 3. \]

EXAMPLE 3 

Using a Prime Factorization

What is the greatest perfect square that is a factor of 1575?

Because 1575 has many factors, it is not efficient to list all of its factors and check for perfect squares. Use the prime factorization of 1575 to find any perfect squares that are factors.

```
1575
25 \cdot 63
5 \cdot 5 \cdot 7 \cdot 3
3 \cdot 3
```

1575 = 3 \cdot 3 \cdot 5 \cdot 5 \cdot 7

The prime factorization shows that 1575 has three factors other than 1 that are perfect squares.

3 \cdot 3 = 9 \\
5 \cdot 5 = 25 \\
(3 \cdot 5) \cdot (3 \cdot 5) = 15 \cdot 15 = 225

\[ \text{So, the greatest perfect square that is a factor of 1575 is 225.} \]

On Your Own

Write the prime factorization of the number.

5. 20 
6. 88 
7. 90 
8. 462 
9. What is the greatest perfect square that is a factor of 396? Explain.
1.4 Exercises

**Vocabulary and Concept Check**

1. **VOCABULARY** What is the prime factorization of a number?
2. **VOCABULARY** How can you use a factor tree to help you write the prime factorization of a number?
3. **WHICH ONE DOESN'T BELONG?** Which factor pair does not belong with the other three? Explain your reasoning.

2, 28
4, 14
6, 9
7, 8

**Practice and Problem Solving**

Use divisibility rules to determine whether the number is divisible by 2, 3, 5, 6, 9, and 10. Use a calculator to check your answer.

4. 1044  
5. 1485  
6. 1620  
7. 1709

List the factor pairs of the number.

8. 15  
9. 22  
10. 34  
11. 39  
12. 45  
13. 54  
14. 59  
15. 61

Write the prime factorization of the number.

16. 16  
17. 25  
18. 30  
19. 26  
20. 84  
21. 54  
22. 65  
23. 77

24. **ERROR ANALYSIS** Describe and correct the error in writing the prime factorization.

25. **FACTOR RAINBOW** You can use a factor rainbow to check whether a list of factors is correct. To create a factor rainbow, list the factors of a number in order from least to greatest. Then draw arches that link the factor pairs. For perfect squares, there is no connecting arch in the middle. So, just circle the middle number. A factor rainbow for 12 is shown. Create factor rainbows for 6, 24, 36, and 48.
Find the number represented by the prime factorization.

26. \(2^2 \cdot 3^2 \cdot 5\)
27. \(3^2 \cdot 5^2 \cdot 7\)
28. \(2^3 \cdot 11^2 \cdot 13\)

Find the greatest perfect square that is a factor of the number.

29. 244
30. 650
31. 756
32. 1290

33. **CRITICAL THINKING** Is 2 the only even prime number? Explain.

34. **BASEBALL** The coach of a baseball team separates the players into groups for drills. Each group has the same number of players. Is the total number of players on the baseball team prime or composite? Explain.

35. **SCAVENGER HUNT** A teacher divides 36 students into equal groups for a scavenger hunt. Each group should have at least 4 students but no more than 8 students. What are the possible group sizes?

36. **PERFECT NUMBERS** A perfect number is a number that equals the sum of its factors, not including itself. For example, the factors of 28 are 1, 2, 4, 7, 14, and 28. Because \(1 + 2 + 4 + 7 + 14 = 28\), 28 is a perfect number. What are the perfect numbers between 1 and 28?

37. **BAKE SALE** One table at a bake sale has 75 cookies. Another table has 60 cupcakes. Which table allows for more rectangular arrangements when all the cookies and cupcakes are displayed? Explain.

38. **MODELING** The stage manager of a school play creates a rectangular acting area of 42 square yards. String lights will outline the acting area. To the nearest whole number, how many yards of string lights does the manager need to enclose this area?

39. **Volume** The volume of a rectangular prism can be found using the formula \(volume = length \times width \times height\). Using only whole number dimensions, how many different prisms are possible? Explain.

**Fair Game Review** What you learned in previous grades & lessons

Find the difference. *(Skills Review Handbook)*

40. 192 – 47
41. 451 – 94
42. 3210 – 815
43. 4752 – 3504

44. **MULTIPLE CHOICE** You buy 168 pears. There are 28 pears in each bag. How many bags of pears do you buy? *(Skills Review Handbook)*

\[\text{A} \quad 5 \quad \text{B} \quad 6 \quad \text{C} \quad 7 \quad \text{D} \quad 28\]
**Essential Question** How can you find the greatest common factor of two numbers?

A **Venn diagram** uses circles to describe relationships between two or more sets. The Venn diagram shows the names of students enrolled in two activities. Students enrolled in both activities are represented by the overlap of the two circles.

![Venn diagram with students' names and overlaps](image)

1. **ACTIVITY: Identifying Common Factors**

   Work with a partner. Copy and complete the Venn diagram. Identify the common factors of the two numbers.

   a. 36 and 48
   b. 16 and 56
   c. 30 and 75
   d. 54 and 90
   e. Look at the Venn diagrams in parts (a)–(d). Explain how to identify the greatest common factor of each pair of numbers. Then circle it in each diagram.
2. **ACTIVITY: Interpreting a Venn Diagram of Prime Factors**

Work with a partner. The Venn diagram represents the prime factorization of two numbers. Identify the two numbers. Explain your reasoning.

a. 

![Venn diagram with 2, 3, and 3 overlapping]

b. 

![Venn diagram with 2, 3, 3, 2, 5, and 11]

3. **ACTIVITY: Identifying Common Prime Factors**

Work with a partner.

a. Write the prime factorizations of 36 and 48. Use the results to complete the Venn diagram.

![Venn diagram with prime factors of 36 and 48]

b. Repeat part (a) for the remaining number pairs in Activity 1.

c. **STRUCTURE** Compare the numbers in the overlap of the Venn diagrams to your results in Activity 1. What conjecture can you make about the relationship between these numbers and your results in Activity 1?

**What Is Your Answer?**

4. **IN YOUR OWN WORDS** How can you find the greatest common factor of two numbers? Give examples to support your explanation.

5. Can you think of another way to find the greatest common factor of two numbers? Explain.

Use what you learned about greatest common factors to complete Exercises 4–6 on page 34.
Factors that are shared by two or more numbers are called **common factors**. The greatest of the common factors is called the **greatest common factor** (GCF). One way to find the GCF of two or more numbers is by listing factors.

**EXAMPLE 1** Finding the GCF Using Lists of Factors

Find the GCF of 24 and 40.

List the factors of each number.

Factors of 24: \(1, 2, 3, 4, 6, 8, 12, 24\)

Factors of 40: \(1, 2, 4, 5, 8, 10, 20, 40\)

The common factors of 24 and 40 are 1, 2, 4, and 8. The greatest of these common factors is 8.

*: So, the GCF of 24 and 40 is 8.

Another way to find the GCF of two or more numbers is by using prime factors. The GCF is the product of the common prime factors of the numbers.

**EXAMPLE 2** Finding the GCF Using Prime Factorizations

Find the GCF of 12 and 56.

Make a factor tree for each number.

\[
\begin{align*}
12 & = 2 \cdot 2 \cdot 3 \\
56 & = 2 \cdot 2 \cdot 2 \cdot 7
\end{align*}
\]

Write the prime factorization of each number.

\[
\begin{align*}
12 & = 2 \cdot 2 \cdot 3 \\
56 & = 2 \cdot 2 \cdot 2 \cdot 7
\end{align*}
\]

*: So, the GCF of 12 and 56 is 4.

**On Your Own**

Find the GCF of the numbers using lists of factors.

1. 8, 36
2. 18, 72
3. 14, 28, 49

Find the GCF of the numbers using prime factorizations.

4. 20, 45
5. 32, 90
6. 45, 75, 120
EXAMPLE 3  Finding Two Numbers with a Given GCF

Which pair of numbers has a GCF of 15?

A 10, 15  B 30, 60  C 21, 45  D 45, 75

The number 15 cannot be a factor of the lesser number 10. So, you can eliminate Statement A.

The number 15 cannot be a factor of a number that does not have a 0 or 5 in the ones place. So, you can eliminate Statement C.

List the factors for Statements B and D. Then identify the GCF for each.

Choice B: Factors of 30: 1, 2, 3, 5, 6, 10, 15, 30
Factors of 60: 1, 2, 3, 4, 5, 6, 10, 12, 15, 20, 30, 60
The GCF of 30 and 60 is 30.

Choice D: Factors of 45: 1, 3, 5, 9, 15, 45
Factors of 75: 1, 3, 5, 15, 25, 75
The GCF of 45 and 75 is 15.

The correct answer is D.

EXAMPLE 4  Real-Life Application

You are filling piñatas for your sister’s birthday party. The list shows the gifts you are putting into the piñatas. You want identical groups of gifts in each piñata with no gifts left over. What is the greatest number of piñatas you can make?

The GCF of the numbers of gifts represents the greatest number of identical groups of gifts you can make with no gifts left over. So, to find the number of piñatas, find the GCF.

Find the product of the common prime factors.

The GCF of 18, 24, and 42 is 6.

So, you can make at most 6 piñatas.

On Your Own

7. Write a pair of numbers whose greatest common factor is 10.

8. WHAT IF? In Example 4, you add 6 more pairs of earrings. Does this change your answer? Explain your reasoning.
1. **VOCABULARY** What is the greatest common factor (GCF) of two numbers?

2. **WRITING** Describe how to find the GCF of two numbers by using prime factorization.

3. **DIFFERENT WORDS, SAME QUESTION** Which is different? Find “both” answers.
   - What is the greatest common factor of 24 and 32?
   - What is the greatest common divisor of 24 and 32?
   - What is the greatest prime factor of 24 and 32?
   - What is the product of the common prime factors of 24 and 32?

4. Use a Venn diagram to find the greatest common factor of the numbers.
   - 4. 12, 30
   - 5. 32, 54
   - 6. 24, 108

5. Find the GCF of the numbers using lists of factors.
   - 7. 6, 15
   - 8. 14, 84
   - 9. 45, 76
   - 10. 39, 65
   - 11. 51, 85
   - 12. 40, 63

6. Find the GCF of the numbers using prime factorizations.
   - 13. 45, 60
   - 14. 27, 63
   - 15. 36, 81
   - 16. 72, 84
   - 17. 61, 73
   - 18. 189, 200

7. **ERROR ANALYSIS** Describe and correct the error in finding the GCF.
   - 19. \[ 42 = 2 \cdot 3 \cdot 7 \]
   - \[ 154 = 2 \cdot 7 \cdot 11 \]
   - The GCF is 7.
   - \[ 36 = 2^2 \cdot 3^2 \]
   - \[ 60 = 2^2 \cdot 3 \cdot 5 \]
   - The GCF is \[ 2 \cdot 3 = 6. \]

8. **CLASSROOM** A teacher is making identical activity packets using 92 crayons and 23 sheets of paper. What is the greatest number of packets the teacher can make with no items left over?

9. **BALLOONS** You are making balloon arrangements for a birthday party. There are 16 white balloons and 24 red balloons. Each arrangement must be identical. What is the greatest number of arrangements you can make using every balloon?
Find the GCF of the numbers.

23. 35, 56, 63  
24. 30, 60, 78  
25. 42, 70, 84

26. OPEN-ENDED Write a set of three numbers that have a GCF of 16. What procedure did you use to find your answer?

27. REASONING You need to find the GCF of 256 and 400. Would you rather list their factors or use their prime factorizations? Explain.

CRITICAL THINKING Tell whether the statement is always, sometimes, or never true.

28. The GCF of two even numbers is 2.
29. The GCF of two prime numbers is 1.
30. When one number is a multiple of another, the GCF of the numbers is the greater of the numbers.

31. BOUQUETS A florist is making identical bouquets using 72 red roses, 60 pink roses, and 48 yellow roses. What is the greatest number of bouquets that the florist can make if no roses are left over? How many of each color are in each bouquet?

32. VENN DIAGRAM Consider the numbers 252, 270, and 300.
   a. Create a Venn diagram using the prime factors of the numbers.
   b. Use the Venn diagram to find the GCF of 252, 270, and 300.
   c. What is the GCF of 252 and 270? 252 and 300? Explain how you found your answer.

33. FRUIT BASKETS You are making fruit baskets using 54 apples, 36 oranges, and 73 bananas.
   a. Explain why you cannot make identical fruit baskets without leftover fruit.
   b. What is the greatest number of identical fruit baskets you can make with the least amount of fruit left over? Explain how you found your answer.

34. Problem Solving Two rectangular, adjacent rooms share a wall. One-foot-by-one-foot tiles cover the floor of each room. Describe how the greatest possible length of the adjoining wall is related to the total number of tiles in each room. Draw a diagram that represents one possibility.

**Fair Game Review** What you learned in previous grades & lessons

Tell which property is being illustrated. *(Skills Review Handbook)*

35. $13 + (29 + 7) = 13 + (7 + 29)$  
36. $13 + (7 + 29) = (13 + 7) + 29$  
37. $(6 \times 37) \times 5 = (37 \times 6) \times 5$  
38. $(37 \times 6) \times 5 = 37 \times (6 \times 5)$

39. MULTIPLE CHOICE In what order should you perform the operations in the expression $4 \times 3 - 12 \div 2 + 5$? *(Section 1.3)*
   
   A $\times, -, \div, +$  
   B $\times, \div, +, -$  
   C $\times, +, -, -$  
   D $\times, +, -, +$
Essential Question: How can you find the least common multiple of two numbers?

ACTIVITY: Identifying Common Multiples

Work with a partner. Using the first several multiples of each number, copy and complete the Venn diagram. Identify any common multiples of the two numbers.

a. 8 and 12

b. 4 and 14

c. 10 and 15

d. 20 and 35

e. Look at the Venn diagrams in parts (a)–(d). Explain how to identify the least common multiple of each pair of numbers. Then circle it in each diagram.
Work with a partner.

a. Write the prime factorizations of 8 and 12. Use the results to complete the Venn diagram.

b. Repeat part (a) for the remaining number pairs in Activity 1.

c. STRUCTURE Compare the numbers from each section of the Venn diagrams to your results in Activity 1. What conjecture can you make about the relationship between these numbers and your results in Activity 1?

What Is Your Answer?

3. IN YOUR OWN WORDS How can you find the least common multiple of two numbers? Give examples to support your explanation.

4. The Venn diagram shows the prime factors of two numbers.

Use the diagram to do the following tasks.

a. Identify the two numbers.

b. Find the greatest common factor.

c. Find the least common multiple.

5. A student writes the prime factorizations of 8 and 12 in a table as shown. She claims she can use the table to find the greatest common factor and the least common multiple of 8 and 12. How is this possible?

6. Can you think of another way to find the least common multiple of two or more numbers? Explain.

Use what you learned about least common multiples to complete Exercises 3–5 on page 40.
Multiples that are shared by two or more numbers are called **common multiples**. The least of the common multiples is called the **least common multiple** (LCM). You can find the LCM of two or more numbers by listing multiples or using prime factors.

### EXAMPLE 1 Finding the LCM Using Lists of Multiples

Find the LCM of 4 and 6.

List the multiples of each number.

- **Multiples of 4**: 4, 8, 12, 16, 20, 24, 28, 32, 36, ...  
- **Multiples of 6**: 6, 12, 18, 24, 30, 36, ...  

Some common multiples of 4 and 6 are 12, 24, and 36. The least of these common multiples is 12.

∴ So, the LCM of 4 and 6 is 12.

### On Your Own

Find the LCM of the numbers using lists of multiples.

1. 3, 8
2. 9, 12
3. 6, 10

### EXAMPLE 2 Finding the LCM Using Prime Factorizations

Find the LCM of 16 and 20.

Make a factor tree for each number.

\[
\begin{align*}
16 & = 2 \cdot 2 \cdot 2 \cdot 2 \\
20 & = 2 \cdot 2 \cdot 5
\end{align*}
\]

Write the prime factorization of each number. Circle each different factor where it appears the greater number of times.

- 16 = \(2 \cdot 2 \cdot 2 \cdot 2\)  
  2 appears more often here, so circle all 2s.
- 20 = 2 \cdot 2 \cdot 5  
  5 appears once. Do not circle the 2s again.
- \(2 \cdot 2 \cdot 2 \cdot 2 \cdot 5 = 80\)  
  Find the product of the circled factors.

∴ So, the LCM of 16 and 20 is 80.

### On Your Own

Find the LCM of the numbers using prime factorizations.

4. 14, 18
5. 28, 36
6. 24, 90
EXAMPLE 3 Finding the LCM of Three Numbers

Find the LCM of 4, 15, and 18.

Write the prime factorization of each number. Circle each different factor where it appears the greatest number of times.

\[ 4 = 2 \cdot 2 \]  
\[ 15 = 3 \cdot 5 \]  
\[ 18 = 2 \cdot 3 \cdot 3 \]

2 appears most often here, so circle both 2s.

5 appears here only, so circle 5.

3 appears most often here, so circle both 3s.

\[ 2 \cdot 2 \cdot 5 \cdot 3 \cdot 3 = 180 \]

Find the product of the circled factors.

So, the LCM of 4, 15, and 18 is 180.

On Your Own

Find the LCM of the numbers.

7. 2, 5, 8

8. 6, 10, 12

9. Write a set of numbers whose least common multiple is 100.

EXAMPLE 4 Real-Life Application

A traffic light changes every 30 seconds. Another traffic light changes every 40 seconds. Both lights just changed. After how many minutes will both lights change at the same time again?

Find the LCM of 30 and 40 by listing multiples of each number. Circle the least common multiple.

**Multiples of 30:** 30, 60, 90, 120, . . .

**Multiples of 40:** 40, 80, 120, 160, . . .

The LCM is 120. So, both lights will change again after 120 seconds.

Because there are 60 seconds in 1 minute, there are \[ 120 \div 60 = 2 \] minutes in 120 seconds.

Both lights will change at the same time again after 2 minutes.

On Your Own

10. WHAT IF? In Example 4, the traffic light that changes every 40 seconds is adjusted to change every 45 seconds. Both lights just changed. After how many minutes will both lights change at the same time again?
**Vocabulary and Concept Check**

1. **VOCABULARY** What is the least common multiple (LCM) of two numbers?

2. **WRITING** Describe how to find the LCM of two numbers by using prime factorization.

**Practice and Problem Solving**

Use a Venn diagram to find the least common multiple of the numbers.

3. 3, 7

4. 6, 8

5. 12, 15

Find the LCM of the numbers using lists of multiples.

6. 2, 9

7. 3, 4

8. 8, 9

9. 5, 8

10. 15, 20

11. 12, 18

Find the LCM of the numbers using prime factorizations.

12. 9, 21

13. 12, 27

14. 18, 45

15. 22, 33

16. 36, 60

17. 35, 50

18. **ERROR ANALYSIS** Describe and correct the error in finding the LCM.

\[ 6 \times 9 = 54 \]

The LCM of 6 and 9 is 54.

19. **AQUATICS** You have diving lessons every fifth day and swimming lessons every third day. Today you have both lessons. In how many days will you have both lessons on the same day again?

20. **HOT DOGS** Hot dogs come in packs of 10, while buns come in packs of eight. What are the least numbers of packs you should buy in order to have the same numbers of hot dogs and buns?

21. **MODELING** Which model represents an LCM that is different from the other three? Explain your reasoning.

**A.**

**B.**

**C.**

**D.**

**Chapter 1** Numerical Expressions and Factors
Find the LCM of the numbers.

22. 2, 3, 7
23. 3, 5, 11
24. 4, 9, 12
25. 6, 8, 15
26. 7, 18, 21
27. 9, 10, 28

28. **REASONING** You need to find the LCM of 13 and 14. Would you rather list their multiples or use their prime factorizations? Explain.

**CRITICAL THINKING** Tell whether the statement is *always*, *sometimes*, or *never* true.

29. The LCM of two different prime numbers is their product.
30. The LCM of a set of numbers is equal to one of the numbers in the set.
31. The GCF of two different numbers is the LCM of the numbers.

32. **SUBWAY** At Union Station, you notice that three subway lines just arrived at the same time. The table shows their arrival schedule. How long must you wait until all three lines arrive at Union Station at the same time again?

<table>
<thead>
<tr>
<th>Subway Line</th>
<th>Arrival Time</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>every 10 min</td>
</tr>
<tr>
<td>B</td>
<td>every 12 min</td>
</tr>
<tr>
<td>C</td>
<td>every 15 min</td>
</tr>
</tbody>
</table>

33. **RADIO CONTEST** A radio station gives away $15 to every 15th caller, $25 to every 25th caller, and free concert tickets to every 100th caller. When will the station first give away all three prizes to one caller?

34. **TREADMILL** You and a friend are running on treadmills. You run 0.5 mile every 3 minutes, and your friend runs 2 miles every 14 minutes. You both start and stop running at the same time and run a whole number of miles. What is the least possible number of miles you and your friend can run?

35. **VENN DIAGRAM** Refer to the Venn diagram.
   - a. Copy and complete the Venn diagram.
   - b. What is the LCM of 16, 24, and 40?
   - c. What is the LCM of 16 and 40? 24 and 40?

36. **Number Sense** When is the LCM of two numbers equal to their product?

**Fair Game Review** What you learned in previous grades & lessons

Write the product as a power.  

37. \(3 \times 3\)
38. \(5 \times 5 \times 5\)
39. \(17 \times 17 \times 17 \times 17\)

40. **MULTIPLE CHOICE** Which two powers have the same value?  
   - A  \(1^3\) and \(3^1\)
   - B  \(2^4\) and \(4^2\)
   - C  \(3^2\) and \(2^3\)
   - D  \(4^3\) and \(3^4\)

Section 1.6  Least Common Multiple  41
Recall that you can add and subtract fractions with unlike denominators by writing equivalent fractions with a common denominator. One way to do this is by multiplying the numerator and the denominator of each fraction by the denominator of the other fraction.

**EXAMPLE** 1  Adding Fractions Using a Common Denominator

Find $\frac{5}{8} + \frac{1}{6}$.

Rewrite the fractions with a common denominator. Use the product of the denominators as the common denominator.

$$\frac{5}{8} + \frac{1}{6} = \frac{5 \cdot 6}{8 \cdot 6} + \frac{1 \cdot 8}{6 \cdot 8} = \frac{30}{48} + \frac{8}{48} = \frac{38}{48}$$

Multiply.

$$= \frac{19}{24}$$

Add the numerators.

The least common denominator (LCD) of two or more fractions is the least common multiple (LCM) of the denominators. The LCD provides another method for adding and subtracting fractions with unlike denominators.

**EXAMPLE** 2  Adding Fractions Using the LCD

Find $\frac{5}{8} + \frac{1}{6}$.

Find the LCM of the denominators.

**Multiples of 8:** 8, 16, 24, 32, 40, 48, . . .

**Multiples of 6:** 6, 12, 18, 24, 30, 36, 42, 48, . . .

The LCM of 8 and 6 is 24. So, the LCD is 24.

$$\frac{5}{8} + \frac{1}{6} = \frac{5 \cdot 3}{8 \cdot 3} + \frac{1 \cdot 4}{6 \cdot 4} = \frac{15}{24} + \frac{4}{24} = \frac{19}{24}$$

Add the numerators.
To add or subtract mixed numbers, first rewrite the numbers as improper fractions. Then find the common denominator.

**EXAMPLE 3 Subtracting Mixed Numbers**

Find $4\frac{3}{4} - 2\frac{3}{10}$.

Write the difference using improper fractions.

$$\frac{3}{4} - \frac{3}{10} = \frac{19}{4} - \frac{23}{10}$$

**Method 1:** Use the product of the denominators as the common denominator.

$$\frac{19}{4} - \frac{23}{10} = \frac{19 \cdot 10}{4 \cdot 10} - \frac{23 \cdot 4}{10 \cdot 4}$$

Rewrite the fractions using a common denominator of $4 \cdot 10 = 40$.

$$= \frac{190 - 92}{40}$$

Multiply.

$$= \frac{98}{40}$$

Subtract the numerators.

$$= \frac{49}{20}$$

Simplify.

$$= 2\frac{9}{20}$$

**Method 2:** Use the LCD. The LCM of 4 and 10 is 20.

$$\frac{19}{4} - \frac{23}{10} = \frac{19 \cdot 5}{4 \cdot 5} - \frac{23 \cdot 2}{10 \cdot 2}$$

Rewrite the fractions using the LCD, 20.

$$= \frac{95 - 46}{20}$$

Multiply.

$$= \frac{49}{20}$$

Simplify.

$$= 2\frac{9}{20}$$

**Practice**

Use the LCD to rewrite the fractions with the same denominator.

1. $\frac{1}{6} + \frac{3}{8}$
2. $\frac{4}{7} + \frac{3}{10}$
3. $\frac{5}{12} - \frac{9}{9}$
4. $\frac{3}{4} + \frac{5}{8} - \frac{1}{10}$

Copy and complete the statement using $<$, $>$, or $=$.

5. $\frac{4}{5} \quad \frac{5}{6}$
6. $\frac{5}{14} \quad \frac{3}{8}$
7. $2\frac{2}{5} \quad \frac{24}{10}$
8. $\frac{4}{25} \quad \frac{7}{20}$

Add or subtract. Write the answer in simplest form.

9. $\frac{2}{3} + \frac{3}{4}$
10. $\frac{6}{7} + \frac{1}{2}$
11. $\frac{7}{10} - \frac{5}{12}$
12. $\frac{13}{18} - \frac{5}{8}$

13. $2\frac{1}{6} + \frac{3}{4}$
14. $\frac{3}{16} + \frac{1}{10}$
15. $\frac{5}{6} - \frac{3}{4}$
16. $\frac{2}{3} - \frac{2}{11}$

17. **COMPARING METHODS** List some advantages and disadvantages of each method shown in the examples. Which method do you prefer? Why?
1.4–1.6 Quiz

List the factor pairs of the number. (Section 1.4)
1. 48  
2. 56

Write the prime factorization of the number. (Section 1.4)
3. 60  
4. 72

Find the GCF of the numbers using lists of factors. (Section 1.5)
5. 18, 42  
6. 24, 44, 52

Find the GCF of the numbers using prime factorizations. (Section 1.5)
7. 38, 68  
8. 68, 76, 92

Find the LCM of the numbers using lists of multiples. (Section 1.6)
9. 8, 14  
10. 3, 6, 16

Find the LCM of the numbers using prime factorizations. (Section 1.6)
11. 18, 30  
12. 6, 24, 32

Add or subtract. Write the answer in simplest form. (Section 1.6)
13. \( \frac{3}{5} + \frac{2}{3} \)  
14. \( \frac{7}{8} - \frac{3}{4} \)

15. **PICNIC BASKETS** You are creating identical picnic baskets using 30 sandwiches and 42 cookies. What is the greatest number of baskets that you can fill using all of the food? (Section 1.5)

16. **RIBBON** You have 52 inches of yellow ribbon and 64 inches of red ribbon. You want to cut the ribbons into pieces of equal length with no leftovers. What is the greatest length of the pieces that you can make? (Section 1.5)

17. **MUSIC LESSONS** You have piano lessons every fourth day and guitar lessons every sixth day. Today you have both lessons. In how many days will you have both lessons on the same day again? Explain. (Section 1.6)

18. **HAMBURGERS** Hamburgers come in packs of 20, while buns come in packs of 12. What is the least number of packs you should buy in order to have the same numbers of hamburgers and buns? (Section 1.6)
Review Key Vocabulary

power, p. 12
base, p. 12
exponent, p. 12
perfect square, p. 13
numerical expression, p. 18
evaluate, p. 18
order of operations, p. 18
factor pair, p. 26
prime factorization, p. 26
factor tree, p. 26
Venn diagram, p. 30
common factors, p. 32
greatest common factor (GCF), p. 32
common multiples, p. 38
least common multiple (LCM), p. 38
least common denominator (LCD), p. 42

Review Examples and Exercises

1.1 Whole Number Operations (pp. 2–9)

Use the tens place because 203 is less than 508.

\[
\begin{array}{c}
\text{2} \\
\text{203} \overline{\text{5081}} \\
- \text{406} \\
\text{102} \\
\end{array}
\]

Divide 508 by 203: There are two groups of 203 in 508.
Multiply 2 and 203.
Subtract 406 from 508.

Next, bring down the 1 and divide the ones.

\[
\begin{array}{c}
\text{25 R6} \\
\text{203} \overline{\text{5081}} \\
- \text{406} \\
\text{1021} \\
- \text{1015} \\
\text{6} \\
\end{array}
\]

Divide 1021 by 203: There are five groups of 203 in 1021.
Multiply 5 and 203.
Subtract 1015 from 1021.

The quotient of 5081 and 203 is \(25 \frac{6}{203}\).

Exercises

Find the value of the expression. Use estimation to check your answer.

1. \(4382 + 2899\)  
2. \(8724 - 3568\)  
3. \(192 \times 38\)  
4. \(216 \div 31\)

1.2 Powers and Exponents (pp. 10–15)

Evaluate \(6^2\).

\(6^2 = 6 \times 6 = 36\)  
Write as repeated multiplication and simplify.

Exercises

Find the value of the power.

5. \(7^3\)  
6. \(2^6\)  
7. \(4^4\)
Chapter 1  Numerical Expressions and Factors

1.3 Order of Operations  (pp. 16–21)

Evaluate \(4^3 - 15 \div 5\).

\[
4^3 - 15 \div 5 = 64 - 15 \div 5 \\
= 64 - 3 \\
= 61
\]
Evaluate \(4^3\).
Divide 15 by 5.
Subtract 3 from 64.

Exercises:

Evaluate the expression.

8.  \(3 \times 6 - 12 \div 6\)  
9.  \(20 \times (3^2 - 4) \div 50\)  
10.  \(5 + (4^2 + 2) \div 6\)

1.4 Prime Factorization  (pp. 24–29)

Write the prime factorization of 18.

Find a factor pair and draw "branches."
Circle the prime factors as you find them.
Continue until each branch ends at a prime factor.

The prime factorization of 18 is \(2 \cdot 3 \cdot 3\), or \(2 \cdot 3^2\).

Exercises:

List the factor pairs of the number.

11. 28  
12. 44  
13. 63

Write the prime factorization of the number.

14. 42  
15. 50  
16. 66

1.5 Greatest Common Factor  (pp. 30–35)

a. Find the GCF of 32 and 76.

Factors of 32: 1, 2, 4, 8, 16, 32  
Factors of 76: 1, 2, 4, 19, 38, 76  
The greatest of the common factors is 4.

\[
45 = 3 \cdot 3 \cdot 5 \\
63 = 3 \cdot 3 \cdot 7 \\
\]
So, the GCF of 32 and 76 is 4.

b. Find the GCF of 45 and 63.

Exercises: 11. 28  
12. 44  
13. 63

Write the prime factorization of the number.

14. 42  
15. 50  
16. 66

1.5 Greatest Common Factor  (pp. 30–35)

a. Find the GCF of 32 and 76.

Factors of 32: 1, 2, 4, 8, 16, 32  
Factors of 76: 1, 2, 4, 19, 38, 76  
The greatest of the common factors is 4.

\[
45 = 3 \cdot 3 \cdot 5 \\
63 = 3 \cdot 3 \cdot 7 \\
\]
So, the GCF of 32 and 76 is 4.

b. Find the GCF of 45 and 63.

Exercises: 11. 28  
12. 44  
13. 63

Write the prime factorization of the number.

14. 42  
15. 50  
16. 66

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Chapter Review

### Exercises

Find the GCF of the numbers using lists of factors.

17. 27, 45  
18. 30, 48  
19. 28, 48, 64

Find the GCF of the numbers using prime factorizations.

20. 24, 90  
21. 52, 68  
22. 32, 56, 96

#### 1.6 Least Common Multiple (pp. 36–43)

**a.** Find the LCM of 8 and 12.

Make a factor tree for each number.

\[
\begin{align*}
8 &= 2 \cdot 4 \\
&= 2 \cdot 2 \cdot 2 \\
12 &= 2 \cdot 6 \\
&= 2 \cdot 2 \cdot 3
\end{align*}
\]

Write the prime factorization of each number. Circle each different factor where it appears the greater number of times.

\[
\begin{align*}
8 &= 2 \cdot 2 \cdot 2 \\
&\quad \text{2 appears more often here, so circle all 2s.} \\
12 &= 2 \cdot 2 \cdot 3 \\
&\quad \text{3 appears once. Do not circle the 2s again.} \\
2 \cdot 2 \cdot 2 \cdot 3 &= 24 \\
&\quad \text{Find the product of the circled factors.}
\end{align*}
\]

\[\therefore \text{So, the LCM of 8 and 12 is 24.}\]

**b.** Find \(\frac{1}{2} + \frac{1}{3}\).

The LCM of 2 and 3 is 6. So, the LCD is 6.

\[
\frac{1}{2} + \frac{1}{3} = \frac{1 \cdot 3}{2 \cdot 3} + \frac{1 \cdot 2}{3 \cdot 2} = \frac{3}{6} + \frac{2}{6} = \frac{5}{6}
\]

### Exercises

Find the LCM of the numbers using lists of multiples.

23. 4, 14  
24. 6, 20  
25. 12, 28

Find the LCM of the numbers using prime factorizations.

26. 6, 45  
27. 10, 12  
28. 18, 27

Add or subtract. Write the answer in simplest form.

29. \(\frac{2}{7} + \frac{1}{4}\)  
30. \(\frac{5}{9} + \frac{3}{8}\)  
31. \(\frac{5}{6} - \frac{7}{15}\)

32. **WATER PITCHER** A water pitcher contains \(\frac{2}{3}\) gallon of water. You add \(\frac{5}{7}\) gallon of water to the pitcher. How much water does the pitcher contain?
Find the value of the expression. Use estimation to check your answer.
1. \(3963 + 2379\)  
2. \(6184 - 2348\)  
3. \(184 \times 26\)  
4. \(207 \div 23\)

Find the value of the power.
5. \(2^3\)  
6. \(15^2\)  
7. \(5^4\)

Evaluate the expression.
8. \(11 \times 8 - 6 \div 2\)  
9. \(5 + 2^3 - 4 - 2\)  
10. \(6 + 4(11 - 2) \div 3^2\)

List the factor pairs of the number.
11. 52  
12. 66

Write the prime factorization of the number.
13. 46  
14. 28

Find the GCF of the numbers using lists of factors.
15. 24, 54  
16. 16, 32, 72

Find the GCF of the numbers using prime factorizations.
17. 52, 65  
18. 18, 45, 63

Find the LCM of the numbers using lists of multiples.
19. 14, 21  
20. 9, 24

Find the LCM of the numbers using prime factorizations.
21. 26, 39  
22. 6, 12, 14

23. **BRACELETS** You have 16 yellow beads, 20 red beads, and 24 orange beads to make identical bracelets. What is the greatest number of bracelets that you can make using all the beads?

24. **MARBLES** A bag contains equal numbers of green and blue marbles. You can divide all the green marbles into groups of 12 and all the blue marbles into groups of 16. What is the least number of each color of marble that can be in the bag?

25. **SCALE** You place a 3 \(\frac{3}{8}\)-pound weight on the left side of a balance scale and a 1 \(\frac{1}{5}\)-pound weight on the right side. How much weight do you need to add to the right side to balance the scale?
1. You are making identical bagel platters using 40 plain bagels, 30 raisin bagels, and 24 blueberry bagels. What is the greatest number of platters that you can make if there are no leftover bagels?

A. 2  
B. 6  
C. 8  
D. 10

2. The top of an end table is a square with a side length of 16 inches. What is the area of the tabletop?

F. 16 in.$^2$  
G. 32 in.$^2$  
H. 64 in.$^2$  
I. 256 in.$^2$

3. Which number is equivalent to the expression below?

$3 \cdot 2^3 - 8 \div 4$

A. 0  
B. 4  
C. 22  
D. 214

4. What is the least common multiple of 14 and 49?
5. Which number is equivalent to the expression $7059 \div 301$?
   
   F. $23$
   
   H. $23\frac{136}{301}$
   
   G. $23\frac{136}{7059}$
   
   I. $136$

6. You are building identical displays for the school fair using 65 blue boxes and 91 yellow boxes. What is the greatest number of displays you can build using all the boxes?
   
   A. 13
   
   B. 35
   
   C. 91
   
   D. 156

7. You hang the two strands of decorative lights shown below.

   **Strand 1:** changes between red and blue every 15 seconds
   
   **Strand 2:** changes between green and gold every 18 seconds

   Both strands just changed color. After how many seconds will the strands change color at the same time again?
   
   F. 3 seconds
   
   G. 30 seconds
   
   H. 90 seconds
   
   I. 270 seconds

8. Which expression is equivalent to $\frac{29}{63}$?
   
   A. $\frac{28}{60} + \frac{1}{3}$
   
   B. $\frac{4}{27} + \frac{25}{36}$
   
   C. $\frac{5}{21} + \frac{2}{9}$
   
   D. $\frac{22}{47} + \frac{7}{16}$

9. Which expression is *not* equivalent to 32?
   
   F. $6^2 - 8 \div 2$
   
   G. $30 \div 2 + 5^2 - 8$
   
   H. $30 + 4^2 \div (2 + 6)$
   
   I. $8^2 \div 4 - 2$

10. Which number is equivalent to the expression $148 \times 27$?
    
    A. 3696
    
    B. 3896
    
    C. 3946
    
    D. 3996
11. You have 60 nickels, 48 dimes, and 42 quarters. You want to divide the coins into identical groups with no coins left over. What is the greatest number of groups that you can make?

12. Erica was evaluating the expression in the box below.

\[
\frac{56 \div (2^3 - 1) \times 4}{8} = 56 \div (8 - 1) \times 4
\]

\[
= 56 \div 7 \times 4
\]

\[
= 56 \div 28
\]

\[
= 2
\]

What should Erica do to correct the error that she made?

F. Divide 56 by 8 because operations are performed left to right.

G. Multiply 1 by 4 because multiplication is done before subtraction.

H. Divide 56 by 7 because operations are performed left to right.

I. Divide 56 by 8 and multiply 1 by 4 because division and multiplication are performed before subtraction.

13. Find the greatest common factor for each pair of numbers.

- 10 and 15
- 10 and 21
- 15 and 21

What can you conclude about the greatest common factor of 10, 15, and 21? Explain your reasoning.

14. Which number is not a perfect square?

A. 64
B. 81
C. 96
D. 100

15. Which number pair has a least common multiple of 48?

F. 4, 12
G. 6, 8
H. 8, 24
I. 16, 24

16. Which number is equivalent to the expression below?

\[
\frac{3(6 + 2^2) + 2}{8}
\]

A. 3
B. 4
C. 7
D. 24 \frac{1}{4}