# Advanced Math Unit 2: Operations with Fractions 

Content Area: Mathematics<br>Course(s): Mathematics 5<br>Time Period: December<br>Length: 9 weeks - 45 Instructional Days<br>Status:<br>Published

## Unit Overview

Students will develop conceptual understanding and with accuracy and efficiency solve addition and subtraction of fractions and mixed numbers. Students will also develop an understanding of the multiplication and division of fractions. This unit will be completed in 9 weeks.

## Priority Standards

MATH.6.NS.A. 1

MATH.5.NBT.A. 4
MATH.6.NS.B. 2
MATH.5.NBT.B. 6

MATH.6.NS.B. 3

MATH.5.NBT.B. 7

MATH.5.NF.A
MATH.5.NF.A. 1

MATH.5.NF.A. 2

MATH.5.NF.B

MATH.5.NF.B. 3

Interpret and compute quotients of fractions, and solve word problems involving division of fractions by fractions, e.g., by using visual fraction models and equations to represent the problem.

Use place value understanding to round decimals to any place.
With accuracy and efficiency, divide multi-digit numbers using the standard algorithm.
Find whole-number quotients of whole numbers with up to four-digit dividends and twodigit divisors, using strategies based on place value, the properties of operations, and/or the relationship between multiplication and division. Illustrate and explain the calculation by using equations, rectangular arrays, and/or area models.

With accuracy and efficiency, add, subtract, multiply, and divide multi-digit decimals using the standard algorithm for each operation.

Add, subtract, multiply, and divide decimals to hundredths, using concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction; relate the strategy to a written method and explain the reasoning used.

Use equivalent fractions as a strategy to add and subtract fractions
Add and subtract fractions with unlike denominators (including mixed numbers) by replacing given fractions with equivalent fractions in such a way as to produce an equivalent sum or difference of fractions with like denominators.

Solve word problems involving addition and subtraction of fractions referring to the same whole, including cases of unlike denominators, e.g., by using visual fraction models or equations to represent the problem. Use benchmark fractions and number sense of fractions to estimate mentally and assess the reasonableness of answers.

Apply and extend previous understandings of multiplication and division to multiply and divide fractions

Interpret a fraction as division of the numerator by the denominator ( $a / b=a \div b$ ). Solve word problems involving division of whole numbers leading to answers in the form of fractions or mixed numbers, e.g., by using visual fraction models or equations to represent the problem.

Apply and extend previous understandings of multiplication to multiply a fraction or whole number by a fraction.

MATH.5.NF.B.4.a

MATH.5.NF.B.4.b

MATH.5.NF.B. 5
MATH.5.NF.B.5.a

MATH.5.NF.B.5.b

MATH.5.NF.B. 6

MATH.5.NF.B. 7

MATH.5.NF.B.7.b
MATH.5.NF.B.7.c

Interpret the product $(a / b) \times q$ as $a$ parts of a partition of $q$ into $b$ equal parts; equivalently, as the result of a sequence of operations $a \times q \div b$.

Find the area of a rectangle with fractional side lengths by tiling it with unit squares of the appropriate unit fraction side lengths, and show that the area is the same as would be found by multiplying the side lengths. Multiply fractional side lengths to find areas of rectangles, and represent fraction products as rectangular areas.

Interpret multiplication as scaling (resizing), by:
Comparing the size of a product to the size of one factor on the basis of the size of the other factor, without performing the indicated multiplication.
Explaining why multiplying a given number by a fraction greater than 1 results in a product greater than the given number (recognizing multiplication by whole numbers greater than 1 as a familiar case); explaining why multiplying a given number by a fraction less than 1 results in a product smaller than the given number; and relating the principle of fraction equivalence $a / b=(n \times a) /(n \times b)$ to the effect of multiplying $a / b$ by 1 .

Solve real world problems involving multiplication of fractions and mixed numbers, e.g., by using visual fraction models or equations to represent the problem.

Apply and extend previous understandings of division to divide unit fractions by whole numbers and whole numbers by unit fractions.

Interpret division of a whole number by a unit fraction, and compute such quotients.
Solve real world problems involving division of unit fractions by non-zero whole numbers and division of whole numbers by unit fractions, e.g., by using visual fraction models and equations to represent the problem.

## Unit Learning Goals \& Targets

## CCS Priority Standards

MA.5.5.NF.A Use equivalent fractions as a strategy to add and subtract fractions.

MA.5.5.NF.A. 1 Add and subtract fractions with unlike denominators (including mixed numbers) by replacing given fractions with equivalent fractions in such a way as to produce an equivalent sum or difference of fractions with like denominators.

MA.5.5.NF.A. 2 Solve word problems involving addition and subtraction of fractions referring to the same whole, including cases of unlike denominators, eg., by using visual fraction models or equations to represent the problem. Use benchmark fractions and number sense of fractions to estimate mentally and assess the reasonableness of answers.

MA.5.5.NF.B. 3 Interpret a fraction as division of the numerator by the denominator $(a / b=a$ divided $b y b)$. Solve word problems involving division of whole numbers leading to answers in the form of fractions or mixed numbers, eg., by using visual fraction models or equations to represent the problem.

MA.5.5.NF.B. 4 Apply and extend previous understandings of multiplication to multiply a fraction or a whole number by a

MA.5.5.NF.4a Interpret the product $(a / b) x q$ as parts of a partition of $q$ into $b$ equal parts; equivalently, as a result of a sequence of operations a $\times \mathrm{q} / \mathrm{b}$.

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MA.5.5.NF.4b Find the area of a rectangle with fractional side lengths by tiling it with unit squares of the appropriate unit fraction side lengths, and show that the area is the same as would be found by multiplying the side lengths. Multiply fractional side lengths to find areas of rectangles, and represent fraction products as rectangular areas.

MA.5.5.NF. 5 Interpret multiplication as scaling.
MA.5.5.NF.5a Comparing the size of a product to the size of one factor on the basis of the size of the other factor, without performing the indicated multiplication.

MA.5.5.NF.5b Explaining why multiplying a given number by a fraction greater than 1 results in a product greater than the given number (recognizing multiplication by whole numbers greater than 1 as a familar case); explain why multiplying a given number by a fraction less than 1 results in a product smaller than the given number; and relating the principle of fraction equivalence $a / b=(n \times a) /(n \times b)$ to the effect of multiplying $a / b$ by 1 .

MA.5.5.NF. 6 Solve real world problems involving multiplication of fractions and mixed numbers, eg., by using visual fraction models or equations to represent the problem.

MA.5.5.NF. 7 Apply and extend previous understandings of division to divide unit fractions by whole numbers and whole numbers by unit fractions.

MA.5.5.NF.7a Interpret division of a unit fraction by a non-zero whole number, and compute such quotients.

MA.5.5.NF.7b Interpret division of a whole number by a unit fraction, and compute such quotients.

MA.5.5.NF.7c Solve real world problems involving division of unit fractions by non-zero whole numbers and division of whole numbers by unit fractions, eg., by using visual fraction models and equations to represent the problem.
MATH.6.NS.B. 2 With accuracy and efficiency, divide multi-digit numbers using the standard algorithm.

# MATH.6.NS.B. 3 With accuracy and efficiency, add, subtract, multiply, and divide multi-digit decimals using the standard algorithm for each operation. 

MATH.6.NS.A. 1 Interpret and compute quotients of fractions, and solve word problems involving division of fractions by fractions, e.g., by using visual fraction models and equations to represent the problem.

## Essential Questions

Here you will use the "list" tab at the top to add all essential questions that tie to the priority standards you identified.

- How can properties help you add fraction with unlike denominators?
- How can the strategy draw a diagram help you solve fraction division problems by writing a multiplication sentence?
- How can the strategy work backward help solve a problem with fraciond that involves addition and subtraction?
- How can you add and subtract mixed numbers wit unlike denominators?
- How can you divide fractions by solving a related multiplication sentence?
- How can you find a fractional part of a group?
- How can you find the product of a fraction and a whole number without using a model?
- How can you make reasonable estimates of fraction sums and differences?
- How can you rewrite a pair of fractions so that they have a common denominator?
- How can you use a common denominator to add and subtract fractions with unlike denominators?
- How can you use a model to show the product of a fraction and a whole number?
- How can you use a unit tile to find the area of a rectangle with fractional side lengths?
- How can you use addition or subtraction to describe a pattern or create a sequence with fractions?
- How can you use an area model to show the product of two fractions?
- How can you use diagrams, equations, and story problems to represent division?
- How can you use models to add fractions that have different denominators?
- How can you use models to subtract fractions that have different denominators?
- How can you use renaming to find the difference of two mixed numbers?
- How can you use the strategy guess, check, and revise to solve problems with fractions?
- How do you calculate unit rate?
- How do you complete ratio tables?
- How do you divide a whole number b a fraction and divide a fraction by a whole number?
- How do you divide mixed numbers?
- How do you multiply fractions?
- How do you multiply mixed numbers?
- How do you write a ratio?
- How does a fraction represent division?
- How does the size of the product compare to the size of one factor when multiplying fractions greater than one?
- How does the size of the product compare to the size of one factor when multiplying fractions?


## Materials and Resources

- Assessment Guide
- GoMath Performance Tasks
- Linklt! Standards Assessments
- Renlearnling Performance Tasks
- Think Central Access


## Unit Assessments (Required)

- Big Ideas Grade 5 and 6 Assessments
- I Ready


## Learning Plan and Pacing Guide

| Time Frame | Lesson | Standard(s) | Target |
| :--- | :--- | :--- | :--- |
| Chapter 6 | Chapter 6 Opener: <br> D3 days | Pivide Whole <br> Numbers | Vocabulary |$\quad$ Uask Preview \& $\quad$ Use multiplication to divid

Lesson 6.5: Use Partial
Quotients to Divide by 5.NBT.B.6 Use an area model and par
Two-Digit Numbers
Lesson 6.6: Use Partial
Quotients with a 5.NBT.B. 6 Use partial quotients to div
Remainder
End of Chapter 6:
Divide Whole Day 2 Centers
Numbers
End of Chapter 6:
Divide Whole Day 3 Chapter Assessment
Numbers
With accuracy and efficiency, di algorithm.

Gr 6 Ch 2 lesson 2.6
MATH.6.NS.B. 2


Lesson 7.9: Problem
Solving: Decimal
Operations
End of Chapter 7: Day 1 Performance Task \&
Divide Decimals Centers
End of Chapter 7:
Divide Decimals
Gr. 6 ch 2 lesson 2.7 MATH.6.NS.B. 3
Chapter 8 Opener: Add Performance Task Preview \& and Subtract Fractions Vocabulary

## Lesson 8.1: Simplest

Form
Lesson 8.2: Estimate 5.NF.A. 1
Sums and Differences
of Fractions 5.NF.A. 2
Lesson 8.3: Find
Common 5.NF.A. 1
Denominators
Lesson 8.4: Add 5.NF.A. 1
$\begin{array}{ll}\text { Fractions with Unlike } \\ \text { Denominators } & \text { 5.NF.A. } 2\end{array}$
Lesson 8.5: Subtract 5.NF.A.1
Fractions with Unlike
Denominators 5.NF.A. 2
Lesson 8.6: Add Mixed 5.NF.A. 1
Numbers
5.NF.A. 2
5.NF.A. 1

Lesson 8.7: Subtract Mixed Numbers
5.NF.A. 2

Lesson 8.8: Problem
Solving: Fractions
5.NF.A. 2

End of Chapter 8: Add and Subtract Fractions
End of Chapter 8: Add
and Subtract Fractions
Day 1 Performance Task
Day 2 Centers
End of Chapter 8: Add
and Subtract Fractions
Day 3 Chapter Assessment

Chapter 9 Opener: $\quad$ Performance Task Preview \&
Multiply Fractions Vocabulary
5.NF.A. 1

Chapter 9
11 days

Lesson 9.1: Multiply
5.NF.B.4a

Whole Numbers by Fractions
5.NF.B. 6

Solve word problems invol

With accuracy and efficiency, ad decimals using the standard algr

Write fractions in simplest

Estimate sums and differer

Write fractions using a con

Add fractions with unlike (

Subtract fractions with unl

Add mixed numbers with l

Subtract mixed numbers w

Solve multi-step word prok numbers.

Multiply whole numbers b .

Lesson 9.2: Use
Models to Multiply
Fractions by Whole
Numbers
Lesson 9.3: Multiply
Fractions and Whole
Numbers
Lesson 9.4: Use
Models to Multiply
Fractions
Lesson 9.5: Multiply Fractions

Lesson 9.6: Find Areas of Rectangles

Lesson 9.7: Multiply
Mixed Numbers
Lesson 9.8: Compare
Factors and Products
End of Chapter 9:
Multiply Fractions
End of Chapter 9:
Multiply Fractions
gr 6 ch 2 lesson 2.1

Chapter 10 7 days
5.NF.B.4a
5.NF.B. 6
5.NF.B.4a
5.NF.B. 6
5.NF.B.4a
5.NF.B. 6
5.NF.B.4a
5.NF.B. 6
5.NF.B.4b
5.NF.B. 6
5.NF.B. 6
5.NF.B.5a
5.NF.B.5b

Day 1 Performance Task \& Centers

Day 2 Chapter Assessment

Lesson 10.1: Interpret
Fractions as Division
Lesson 10.2: Mixed
Numbers as Quotients
Lesson 10.3: Divide
Whole Numbers by
Unit Fractions
Gr 6 Ch 2 lesson 2.2
Lesson 10.4: Divide
Unit Fractions by
Whole Numbers
Lesson 10.5: Problem
Solving: Fraction
5.NF.B.7c

Division
End of Chapter 10:
Divide Fractions
Day 1 Performance Task \&

End of Chapter 10:
Divide Fractions

Multiply fractions by whol

Multiply fractions and whc

Use models to multiply a f

Multiply a fraction by a fra

Find areas of rectangles.

Multiply a mixed number 1

Compare a product to each

Understand how fractions 1

Understand how mixed nul

Divide whole numbers by

Divide fractions

Divide unit fractions by wl

Solve multi-step word prol fractions.

## Strategies for Multilingual learners

For Spanish speaking, students can use the EdConnect Spanish book. Others need one on one support, vocabulary flashcards, elimination of word problems, picture clues, Google Translate, peer buddy

- Big ideas spanish textbook
- Multilingual Dictionary
- Spanish letters


## Strategies for Enrichment

- Big Ideas Enrichment \& Extension Pages
- Desmos
- Iready Pathway
- Kahn Academy


## Strategies for Students in Need of Intervention

When students struggle with facts: Reflex Math, multiplication chart, flashcards, timed tests

ACES/Struggling
When students struggle with word problems: highlight clue words, underline the question, break down steps, read aloud, review vocabulary

ACES/Struggling

- Constant progress monitoring and use of data driven instruction
- Flexible grouping
- Highlight key words in word problems
- Incorporate centers that focus on mastery of skills for struggling students
- Incorporate centers that focus on skills that need enrichment
- One on one conferencing
- Performance assessments
- Prodigy Math
- Provide manipulatives and visual aids
- Provide opportunities for higher level activities to be completed
- Provide opportunities for independent projects
- Provide written notes/directions
- Tiered activities/lessons
- Use of calculator
- Use of graph paper


## Technology Integration

Math Playground
Khan Academy
Illustrative Mathematics
Prodigy
Learn Zillion
aaamath
Math is Fun
Sheppard Software
Adapted Mind
Internet 4 Classrooms
Academic Skill Builders
Math Play
Class K-12
Greg Tang Math
Figure This
Woot Math
Freckle Education
http://www.mathplayground.com/grade 5 games.html
http://www.khanacademy.cor/math/cc-fifth-grade-math
http://www.illustrativemathematics.org
http://www.prodigygame.com
http://www.learnzillion.com
http://www.aaamath.com/grade5.html
https://www.mathsisfun.com/
http://www.sheppardsoftware.com/math.htm
http://adaptedmind.com
http://internet4classrooms.com
http://arcademicskillbuilders.com
http://www.math-play.com
https://www.classk12.com
https://gregtangmath.com
figurethis.nctm.org/challenges/math index.htm
https://ed.wootmath.com/adaptive-learning
https://www.freckle.com

- 8.1.5.A. 1 Select and use the appropriate digital tools and resources to accomplish a variety of tasks including solving problems.
- 8.1.5.A. 3 Use a graphic organizer to organize information about problem or issue.
- 8.1.5.A. 4 Graph data using a spreadsheet, analyze and produce a report that explains the analysis of the data.
- 8.1.5.A. 5 Create and use a database to answer basic questions.
- 8.1.5.A. 6 Export data from a database into a spreadsheet; analyze and produce a report that explains the analysis to the data.


## 21st Century Life \& Career Ready Practices

- CRP11. Use technology to enhance productivity.
- CRP2. Apply appropriate academic and technical skills.
- CRP4. Communicate clearly and effectively and with reason.
- CRP6. Demonstrate creativity and innovation.
- CRP8. Utilize critical thinking to make sense of problems and persevere in solving them.


## Interdisciplinary Connections

- • Next Gen Science Standards (5. Structure and Properties of Matter Unit have connections to 5.NBT.A.1; 5.NF.B.7; 5.MD.A.1; 5.MD.C.3; 5.MD.C.4)
-     - Reading Connection: RI.5.4. Determine the meaning of general academic and domain-specific words and phrases in a text relevant to a grade 5 topic or subject area.

