

# Ratios, Rates, and Proportions

Content Area: **Math**  
Course(s):  
Time Period: **MP3**  
Length: **45**  
Status: **Published**

## Unit Overview

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Unit Summary	Unit Rationale
<p>Unit 3 focuses on extending the work with unit rates from grade 6, to compute unit rates associated with ratios of fractions. They recognize and represent proportional relationships in multiple ways, deciding whether two quantities are in a proportional relationship. They identify the constant of proportionality in a variety of representations (e.g. tables, graphs, equations, diagrams, and verbal descriptions) and use proportions to solve problems. Grade 7 learners work with proportions as they represent proportional relationships by equations, interpret points on graphs of proportional relationships in context, and use proportional relationships to solve multi step percent and ratio problems.</p>	<p>Unit 3 builds students procedural skill and fluency related to proportional relationships.</p> <p>Also, unit 3 builds upon students prior knowledge of proportional relationships as students procedural skill and fluency related to percent and percent problems. In this unit students also develop conceptual understanding related to this topic.</p>

## NJSLS

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MATH.7.RP.A	Analyze proportional relationships and use them to solve real-world and mathematical problems
MATH.7.RP.A.1	Compute unit rates associated with ratios of fractions, including ratios of lengths, areas and other quantities measured in like or different units.
MATH.7.RP.A.2	Recognize and represent proportional relationships between quantities.
MATH.7.RP.A.2.a	Decide whether two quantities are in a proportional relationship, e.g., by testing for equivalent ratios in a table or graphing on a coordinate plane and observing whether the graph is a straight line through the origin.
MATH.7.RP.A.2.b	Identify the constant of proportionality (unit rate) in tables, graphs, equations, diagrams,

	and verbal descriptions of proportional relationships.
MATH.7.RP.A.2.c	Represent proportional relationships by equations.
MATH.7.RP.A.2.d	Explain what a point $(x, y)$ on the graph of a proportional relationship means in terms of the situation, with special attention to the points $(0, 0)$ and $(1, r)$ where $r$ is the unit rate.
MATH.7.RP.A.3	Use proportional relationships to solve multistep ratio and percent problems.

## Standards for Mathematical Practice

MATH.K-12.2	Reason abstractly and quantitatively
MATH.K-12.3	Construct viable arguments and critique the reasoning of others
MATH.K-12.4	Model with mathematics
MATH.K-12.5	Use appropriate tools strategically
MATH.K-12.6	Attend to precision
MATH.K-12.7	Look for and make use of structure
MATH.K-12.8	Look for and express regularity in repeated reasoning

## Unit Focus

Enduring Understandings	Essential Questions
<ul style="list-style-type: none"> <li>• Equivalent ratios and unit rates can be used to compare ratios and solve problems</li> <li>• A unit rate can be easier to use to solve problems than a ratio of fractions.</li> <li>• Quantities in a proportional relationship can be described by equivalent ratios</li> <li>• Equations in the form <math>y = kx</math> where <math>k</math> is the constant of proportionality, can be used to represent proportional relationships and solve problems.</li> <li>• The graph of a proportional relationship is a straight line through the origin.</li> <li>• By recognizing proportional quantities, you can use what you know about proportional relationships to solve problems.</li> </ul> <p>Equivalent ratios can be used to find the percent of a number. Percent is a ratio out of 100 that relates the ratio of two quantities.</p> <ul style="list-style-type: none"> <li>• The part divided by the whole and the percent divided by 100 are equivalent ratios.</li> <li>• Proportional reasoning can be used to develop the</li> </ul> <p>Equivalent ratios can be used to find the percent of a number. Percent is a ratio out of 100 that relates the ratio of two quantities.</p> <ul style="list-style-type: none"> <li>• The part divided by the whole and the percent divided by 100 are equivalent ratios.</li> </ul>	<ul style="list-style-type: none"> <li>• How are ratios, rates, and unit rates used to solve problems?</li> <li>• Why is it useful to write a ratio of fractions as a unit rate?</li> <li>• How are proportional quantities described by equivalent ratios?</li> <li>• How can you represent a proportional relationship with an equation?</li> <li>• What does the graph of a proportional relationship look like?</li> <li>• How can proportional reasoning help to solve a problem?</li> <li>• How do percents show the relationship between quantities?</li> <li>• How does proportional reasoning relate to percent?</li> <li>• How are percent problems related to proportional reasoning?</li> <li>• How is finding percent error similar to finding percent change?</li> <li>• How are the concepts of percent markup and percent markdown related to the percent equation?</li> <li>• How does simple interest show proportional reasoning and relate to the percent equation?</li> </ul>

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| <ul style="list-style-type: none"><li>● Proportional reasoning can be used to develop the</li></ul> |  |
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## Instructional Focus

### Learning Targets

- Use ratios and rates to describe the relationship between two quantities
  - Find equivalent ratios and use unit rates to solve multi-step problems
  - Find unit rates with ratios of fractions
  - Use unit rates to solve multi-step problems
  - Determine whether quantities are proportional by testing for equivalent ratios
  - Use the constant of proportionality to write equations that represent proportional relationships
  - Use equations to solve problems involving proportional relationships
  - Use a graph to recognize proportionality
  - Identify a constant of proportionality from a graph
  - Interpret a point on a graph of a proportional relationship
  - Explain whether a solution represents a proportional relationship
  - Use representations to find entry points into problems
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- Understand that equivalent rates can be used to find percents
  - Analyze percents of numbers in a real-world context
  - Construct a percent proportion
  - Use a percent proportion to find an unknown part, whole, or percent
  - Understand the relationship between proportional reasoning and percent
  - Interpret the results of a percent equation in a real-life scenario
  - Solve real-world problems involving percent change and percent error.
  - Understand the percent equation and the different ways it can be used
  - Understand and calculate markups and markdowns
  - Relate percent change to percent markup and percent markdown
  - Identify the parts of interest problems and how the values are related
  - Understand what simple interest is and how it is calculated

### Prerequisite Skills

- Find equal ratios
- Ratio reasoning
- Rates
- Proportional relationships

### Common Misconceptions

Conversion of words to symbols. Percents can only be between 1% and 100% but cannot be smaller or bigger. Percents with decimals are already in decimal form. Combining discounts to have one percent instead of working them sequentially. Confuse how to organize the units in ratios and order. Writing ratios with fractions. Scale of a graph. Interchanging x and y values. Scale factor must be a whole number.

### Spiraling For Mastery

Current Unit Content/Skills	Spiral Focus	Activity
Ratios and Rates • Proportional Relationships • Percent • Connect Percent and Proportion	• Ratio Reasoning (Grade 6) • Rates (Grade 6) • Rations and Rates (Grade 7) Proportional Relationships (Grade 7)	Math Diagnostic and Intervention System Activities

### Assessment

Formative Assessment	Summative Assessment
<ul style="list-style-type: none"> <li>• Homework</li> <li>• Lesson Checks</li> <li>• MathXL • Quizzes</li> <li>• Exit Tickets</li> <li>• Lesson Reflections</li> <li>• Performance Tasks</li> </ul>	<ul style="list-style-type: none"> <li>• Topic Tests (Common Assessments)</li> <li>• Unit 3 Benchmark (Link-It)</li> </ul>

### Resources

Key Resources	Supplemental Resources
<ul style="list-style-type: none"> <li>• Savvas EnVision Math 7</li> <li>• <a href="#">Pacing Guide</a></li> </ul>	<ul style="list-style-type: none"> <li>• IXL</li> <li>• Delta Math</li> <li>• Desmos</li> <li>• Khan Academy</li> </ul>

### Career Readiness, Life Literacies, and Key Skills

CRP.K-12.CRP2	Apply appropriate academic and technical skills.
CRP.K-12.CRP4	Communicate clearly and effectively and with reason.
CRP.K-12.CRP8	Utilize critical thinking to make sense of problems and persevere in solving them.
CRP.K-12.CRP11	Use technology to enhance productivity.

## **Interdisciplinary Connections**

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ELA.L.KL.7.2.A	Acquire and use accurately grade-appropriate general academic and domain-specific words and phrases.
ELA.SL.PE.7.1.A	Come to discussions prepared, having read or researched material under study; explicitly draw on that preparation by referring to evidence on the topic, text, or issue to probe and reflect on ideas under discussion.
ELA.SL.PE.7.1.C	Pose questions that elicit elaboration and respond to others' questions and comments with relevant observations and ideas that bring the discussion back on topic as needed.
ELA.SL.PE.7.1.D	Acknowledge new information expressed by others and, when warranted, modify their own views.
6-8.MS-ETS1-3.4	Analyzing and Interpreting Data
6-8.MS-ETS1-3.ETS1.B.1	There are systematic processes for evaluating solutions with respect to how well they meet the criteria and constraints of a problem.
6-8.MS-ETS1-3.ETS1.B.2	Sometimes parts of different solutions can be combined to create a solution that is better than any of its predecessors.