Unit #3: Linear vs. Exponential Models

Content Area: Math

Course(s):

Time Period: December Length: 7 weeks Status: Published

State Mandated Topics Addressed in this Unit

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N/A	N/A

Linear vs. Exponential Models

Learning Objectives

- Objective 1 Understand that a function has one element of the domain assigned to exactly one element of the range.
- Objective 10 Relate the domain of a function to its graph.
- Objective 11 Relate the domain of a function to the quantitative relationship that it describes.
- Objective 12 Calculate the average rate of change of a function from a graph or a function on an interval.
- Objective 13 Interpret the average rate of change.
- Objective 14 Estimate the average rate of change from a graph.
- Objective 15 Graph simple functions by hand showing key features of the graph.
- Objective 16 Graph complicated functions using technology.
- · Objective 17 Graph exponential & logarithmic functions showing intercepts and end behavior
- Objective 18 Graph linear and quadratic functions showing key features including intercepts, maxima and minima.
- Objective 19- Write a function shown as an expression in equivalent forms.
- Objective 2 F(x) denotes the output of f corresponding to the input of x.
- Objective 20 Reveal different properties of a function by expressing it in different forms.
- Objective 21 Use factoring and completing the square on quadratic functions to show zeroes, extreme, values, and symmetry.
- Objective 22 Interpret zeroes, extreme values, and symmetry of a quadratic in context.
- Objective 23 Write a function shown as an expression in equivalent forms.
- Objective 24 Reveal different properties of a function by expressing it in different forms.
- Objective 25 Use the properties of exponents to interpret exponential functions.
- Objective 26 Identify the percent rate of change in an exponential function.

- Objective 27 Classify exponential functions as exponential growth or decay.
- Objective 28 Use factoring and completing the square on quadratic functions to show zeroes, extreme, values, and symmetry.
- Objective 29 Interpret zeroes, extreme values, and symmetry of a quadratic in context.
- Objective 3 The graph of f is the graph of y=f(x).
- Objective 30 Use the properties of exponents to interpret exponential functions.
- Objective 31 Identify the percent rate of change in an exponential function.
- Objective 32 Classify exponential functions as exponential growth or decay.
- Objective 33 Compare properties of two functions represented differently (algebraically, graphically, numerically, verbally)
- Objective 34 Write a function shown as an expression in equivalent forms.
- Objective 35 Reveal different properties of a function by expressing it in different forms.
- Objective 36 Use the properties of exponents to interpret exponential functions.
- Objective 37 Identify the percent rate of change in an exponential function.
- Objective 38 Classify exponential functions as exponential growth or decay.
- Objective 39 Write a function that describes a relationship between two quantities. *Determine an explicit expression, recursive process, or steps for calculations from a given context*
- Objective 4 Use function notation to evaluation functions for inputs in their domain.
- Objective 40 Combine functions using arithmetic operations
- Objective 41 Build a function by combining two functions and relate the resulting functions to a model
- Objective 42 Write arithmetic & geometric sequences recursively
- Objective 43 Write arithmetic & geometric sequences with an explicit formula.
- Objective 44 Model situations using arithmetic & geometric formulas.
- Objective 45 Translate between arithmetic & geometric formulas.
- Objective 46 Distinguish between situations that can be modeled with linear and exponential functions.
- Objective 47 Prove that linear functions grow by equal differences over equal intervals.
- Objective 48 Prove that exponential functions grow by equal factors over equal intervals.
- Objective 49 Recognize situations where one quantity changes at a constant rate relative to another.
- Objective 5 Interpret statements that use function notations in terms of context.
- Objective 50 Recognize situations where a quantity grows or decays by a constant percent rate.
- Objective 51 Construct linear and exponential functions (with a focus on arithmetic and geometric sequences) from a given graph, description of relationship or two input-output pairs
- Objective 52 Observe using graphs that a quantity increasing exponentially eventually exceeds a quantity increasing linearly, quadratically, or a polynomial.
- Objective 53 Observe using tables that a quantity increasing exponentially eventually exceeds a quantity increasing linearly, quadratically, or a polynomial.
- Objective 54 Interpret the parameters of a linear or exponential functions in context.
- Objective 55 -
- Objective 6 Recognize sequences are functions whose domain is a subset of the integers.
- Objective 7 Sketch a graph using the key features of a function.

- Objective 8 Interpret key features from a graph or a table of values. Key features include: intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums; symmetries; end behavior; and periodicity.
- Objective 9 For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. Key features include: intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums; symmetries; end behavior; and periodicity.

Essential Skills

- Essential Skill 1 Artists will be able to understand that a function has one member of the domain assigned to exactly one element of the range. F(x) denotes the output of f corresponding to the input of x. The graph of f is the graph of y=f(x)
- Essential Skill 10 Artists will be able to calculate the average rate of change of a function from a graph or a function on an interval.
- Essential Skill 11 Artists will be able to interpret the average rate of change.
- Essential Skill 12 Artists will be able to estimate the average rate of change from a graph.
- Essential Skill 13 Artists will be able to graph linear and quadratic functions showing key features including intercepts, maxima and minima.
- Essential Skill 14 Artists will be able to graph simple functions by hand showing key features of the graph.
- Essential Skill 15 Artists will be able to graph complicated functions using technology.
- Essential Skill 16 Artists will be able to graph exponential & Department of the showing intercepts and end behavior
- Essential Skill 17 Artists will be able to write a function shown as an expression in equivalent forms.
- Essential Skill 18 Artists will be able to reveal different properties of a function by expressing it in different forms.
- Essential Skill 19 Artists will be able to use factoring and completing the square on quadratic functions to show zeroes, extreme, values, and symmetry.
- Essential Skill 2 Artists will be able to use function notation to evaluation functions for inputs in their domain.
- Essential Skill 20 Artists will be able to interpret zeroes, extreme values, and symmetry of a quadratic in context.
- Essential Skill 21 Artists will be able to write a function shown as an expression in equivalent forms.
- Essential Skill 22 Artists will be able to reveal different properties of a function by expressing it in different forms.
- Essential Skill 23 Artists will be able to use the properties of exponents to interpret exponential functions.
- Essential Skill 24 Artists will be able to identify the percent rate of change in an exponential function.
- Essential Skill 25 Artists will be able to classify exponential functions as exponential growth or decay.
- Essential Skill 26 Artists will be able to compare properties of two functions represented differently (algebraically, graphically, numerically, verbally) Example: given a graph of a quadratic and algebraic expression, say which has the larger maximum.
- Essential Skill 27 Artists will be able to write a function that describes a relationship between two quantities.

- Essential Skill 28 Artists will be able to determine an explicit expression, recursive process, or steps for calculations from a given context.
- Essential Skill 29 Artists will be able to write a function that describes a relationship between two quantities.
- Essential Skill 3 Artists will be able to interpret statements that use function notations in terms of context.
- Essential Skill 30 Artists will be able to combine functions using arithmetic operations.
- Essential Skill 31 Artists will be able to build a function by combining two functions and relate the resulting functions to a model.
- Essential Skill 32 Artists will be able to write arithmetic & amp; geometric sequences recursively.
- Essential Skill 33 Artists will be able to write arithmetic & geometric sequences with an explicit formula.
- Essential Skill 34 Artists will be able to model situations using arithmetic & amp; geometric formulas.
- Essential Skill 35 Artists will be able to translate between the two forms.
- Essential Skill 36 Artists will be able to distinguish between situations that can be modeled with linear and exponential functions.
- Essential Skill 37 Artists will be able to prove that linear functions grow by equal differences over equal intervals.
- Essential Skill 38 Artists will be able to prove that exponential functions grow by equal factors over equal intervals.
- Essential Skill 39 -Artists will be able to distinguish between situations that can be modeled with linear functions and with exponential functions.
- Essential Skill 4 Artists will be able to recognize sequences are functions whose domain is a subset of the integers.
- Essential Skill 40 Artists will be able to recognize situations where one quantity changes at a constant rate relative to another.
- Essential Skill 41 Artists will be able to recognize situations where a quantity grows or decays by a constant percent rate.
- Essential Skill 42 Artists will be able to construct linear and exponential functions (with a focus on arithmetic and geometric sequences) from a given graph, description of relationship or two input-output pairs.
- Essential Skill 43 Artists will be able to observe using graphs that a quantity increasing exponentially eventually exceeds a quantity increasing linearly, quadratically, or a polynomial)
- Essential Skill 44 Artists will be able to observe using tables that a quantity increasing exponentially eventually exceeds a quantity increasing linearly, quadratically, or a polynomial.
- Essential Skill 45 Artists will be able to interpret the parameters of a linear or exponential functions in context.
- Essential Skill 46 Artists will be able to understand that the graph of an equation in two variables is the set of all of its solutions plotted in the coordinate plane.
- Essential Skill 47 Artists will be able to understand that the solution set to an equation in two variables often forms a curve (which could be a line).
- Essential Skill 48 Artists will be able to explain why the solution of f(x)=g(x) is the x coordinate of their intersection.
- Essential Skill 49 Artists will be able to find the solutions approximately using technology to graph the function or create a table of values. Include f(x) & g(x) that are linear, polynomial, rational, absolute value, exponential, and logarithmic
- Essential Skill 5 Artists will be able to sketch a graph using the key features of a function.

- Essential Skill 50 Artists will be able to create an equation that represents relationships between quantities.
- Essential Skill 51 Artists will be able to graph equations on axes with labels and scales.
- Essential Skill 52 Artists will be able to represent solutions of equations, inequalities, and systems to real-world applications.
- Essential Skill 53 Artists will be able to interpret solutions as viable based on the constraints of the application. Example: cannot have negative time
- Essential Skill 54 Artists will be able to explain the steps to solving an equation.
- Essential Skill 55 Artists will be able to construct a viable argument to justify a solution method.
- Essential Skill 6 Artists will be able to interpret key features from a graph or a table of values.
- Essential Skill 7 Key features include: intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums; symmetries; end behavior; and periodicity.
- Essential Skill 8 Artists will be able to relate the domain of a function its graph.
- Essential Skill 9 Artists will be able to relate the domain of a function to the quantitative relationship that it describes.

Standards

MATH.9-12.F.BF.A.1.a	Determine an explicit expression, a recursive process, or steps for calculation from a context.
MATH.9-12.F.BF.A.1.b	Combine standard function types using arithmetic operations.
MATH.9-12.F.BF.A.1.c	Compose functions.
MATH.9-12.F.BF.B.3	Identify the effect on the graph of replacing $f(x)$ by $f(x) + k$, k $f(x)$, $f(kx)$, and $f(x + k)$ for specific values of k (both positive and negative); find the value of k given the graphs. Experiment with cases and illustrate an explanation of the effects on the graph using technology.
MATH.9-12.F.IF.A.1	Understand that a function from one set (called the domain) to another set (called the range) assigns to each element of the domain exactly one element of the range. If f is a function and x is an element of its domain, then $f(x)$ denotes the output of f corresponding to the input x . The graph of f is the graph of the equation $y = f(x)$.
MATH.9-12.F.IF.A.2	Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context.
MATH.9-12.F.IF.B.4	For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship.
MATH.9-12.F.IF.B.5	Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes.
MATH.9-12.F.IF.B.6	Calculate and interpret the average rate of change of a function (presented symbolically or as a table) over a specified interval. Estimate the rate of change from a graph.
MATH.9-12.F.IF.C.7	Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases.
MATH.9-12.F.IF.C.7.a	Graph linear and quadratic functions and show intercepts, maxima, and minima.
MATH.9-12.F.IF.C.7.b	Graph square root, cube root, and piecewise-defined functions, including step functions and absolute value functions.
MATH.9-12.F.IF.C.7.c	Graph polynomial functions, identifying zeros when suitable factorizations are available,

	and showing end behavior.
MATH.9-12.F.IF.C.7.d	Graph rational functions, identifying zeros and asymptotes when suitable factorizations are available, and showing end behavior.
MATH.9-12.F.IF.C.7.e	Graph exponential and logarithmic functions, showing intercepts and end behavior.
MATH.9-12.F.IF.C.7.f	Graph trigonometric functions, showing period, midline, and amplitude.
MATH.9-12.F.IF.C.8	Write a function defined by an expression in different but equivalent forms to reveal and explain different properties of the function.
MATH.9-12.F.IF.C.8.a	Use the process of factoring and completing the square in a quadratic function to show zeros, extreme values, and symmetry of the graph, and interpret these in terms of a context.
MATH.9-12.F.IF.C.8.b	Use the properties of exponents to interpret expressions for exponential functions.
MATH.9-12.F.IF.C.9	Compare properties of two functions each represented in a different way (algebraically, graphically, numerically in tables, or by verbal descriptions).
MATH.9-12.F.LE.A.1	Distinguish between situations that can be modeled with linear functions and with exponential functions.
MATH.9-12.F.LE.A.1.a	Prove that linear functions grow by equal differences over equal intervals, and that exponential functions grow by equal factors over equal intervals.
MATH.9-12.F.LE.A.1.b	Recognize situations in which one quantity changes at a constant rate per unit interval relative to another.
MATH.9-12.F.LE.A.1.c	Recognize situations in which a quantity grows or decays by a constant percent rate per unit interval relative to another.
MATH.9-12.F.LE.A.2	Construct linear and exponential functions, including arithmetic and geometric sequences, given a graph, a description of a relationship, or two input-output pairs (include reading these from a table).
MATH.9-12.F.LE.B.5	Interpret the parameters in a linear or exponential function in terms of a context.

Instructional Tasks/Activities

- Activity Match the graph with the equation.
- Activity (QUIZIZZ)
- Activity 1 Ladder Activity
- Activity 2 Academic games & Competitions
- Activity 3 Worksheets
- Activity 4 Formative Assessments
- Activity 5 Arts inspired projects
- Activity 6 Project: Zombie growth-comparing linear and exponential growth of a population
- Activity in QUIZIZZ (slope- intercept)
- Converting linear graphs into standard form
- Converting standard form into slope-intercept form
- Intro intro to linear functions
- Intro to standard form (linear equations)
- Linear equations Review
- Linear equations Review (standard form)

- Linear equations word problems
- Make-up day on missing assignments, Quizizz, Quiz.
- Practice slope-intercept, standard form and linear graphs
- Quiz
- Solve Linear functions using slope-intercept
- Solve Linear functions using slope-intercept in graphs
- Worksheet on Average rate of change (Review)
- Worksheet on Average rate of change between two points
- Worksheet on Average rate of change in a graph
- Worksheet on Average rate of change of linear functions
- Worksheet on Average rate of change of non-linear functions

Assessment Procedure

- Classroom Total Participation Technique
- Classwork
- DBQ
- Essay
- Exit Ticket/Entrance Ticket/Do Now
- Journal / Student Reflection
- Kahoot
- Other named in lesson
- Peer Review
- Performance
- Problem Correction
- Project
- Quiz
- Rubric
- Teacher Collected Data
- Test
- Worksheet

Recommended Technology Activities

- Appropriate Content Specific Online Resource
- Chromebook
- Gimkit
- GoGuardian
- Google Classroom

- Google Docs
- · Google Forms
- Google Slides
- Kahoot
- MagicSchool Al
- Other- Specified in Lesson
- Quizizz
- Screencastify

Accommodations & Modifications & Differentiation

Accommodations and Modifications should be used to meet individual needs. Their IEP and 504 plans should be used in addition to the following suggestions.

Gifted and Talented

- Compare & Contrast
- Conferencing
- Debates
- Jigsaw
- Peer Partner Learning
- Problem Solving
- Structured Controversy
- Think, Pair, Share
- Tutorial Groups

Instruction/Materials

- alter format of materials (type/highlight, etc.)
- color code materials
- eliminate answers
- extended time
- extended time
- large print
- modified quiz
- modified test
- · Modify Assignments as Needed
- Modify/Repeat/Model directions

- necessary assignments only
- Other (specify in plans)
- other- named in lesson
- provide assistance and cues for transitions
- provide daily assignment list
- read class materials orally
- reduce work load
- shorten assignments
- study guide/outline
- utilize multi-sensory modes to reinforce instruction

Environment

- alter physical room environment
- assign peer tutors/work buddies/note takers
- assign preferential seating
- individualized instruction/small group
- modify student schedule (Describe)
- other- please specify in plans
- provide desktop list/formula

Honors Modifications

Resources

• Resource 1 - www.Khanacademy.com