# Unit 3: Fraction and Decimal Concepts <br> Content Area: Course(s): Time Period: Length: Status: <br> Math <br> Math Gr. 4 <br> JanFeb 24 Days Published 

## Department of Curriculum and Instruction



Belleville Public Schools

# Mathematics: Grade 4 <br> Unit 3: Fraction and Decimal Concepts 

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## Unit Overview

Unit 3 will cover two topics including (T8) Fraction Equivalence and Ordering and (T12) Understand and Compare Decimals.

## Enduring Understandings

## Topic 8 focuses on:

- Two fractions that represent the same part of the same whole are equivalent. The two fractions are different names for the same number.
- The same fractional amount can be represented by an infinite set of different but equivalent fractions.
- When the numerator and denominator of a fraction are multiplied by the same number greater than 1 , it is the same as multiplying the fraction by 1 . This gives an equivalent fraction because multiplying by 1 does not change the value of a number.
- When the numerator and denominator of a fraction are divided by a common factor, the result is an equivalent fraction.
- One way to compare two fractions that are parts of the same whole is by comparing each to a benchmark fraction such as $1 / 2$.
- When two fractions have the same denominator, the fraction with the greater numerator is greater. When two fraction have the same numerator, the fraction with the lesser denominator is greater.
- Good math thinkers use math to explain why they are right. They can talk about the math that others do, too.


## Topic 12 focuses on:

- A decimal is another way to represent a fraction.
- Points on a number line can represent fractions and decimals. A fraction and a decimal tell the distance a point is from 0 on the number line.
- Place value can be used to compare decimals.
- Fractions with denominators of 10 can be written as equivalent fractions with denominators of 100 . Fractions with like denominators can be added.
- Fractions and decimals can be used to represent amounts of money. Pictorial models and equations can represent problems involving money.
- Good math thinkers look for relationships in math to help solve problems.


## Essential Questions

(T8) Fraction Equivalence and Ordering

- What are some ways to name the same part of a whole?
- How can you compare fractions with unlike denominators?
(T12) Understand and Compare Decimals.
- How can you write a fraction as a decimal?
- How can you locate points on a number line?
- How do you compare decimals?


## Exit Skills

Topics 8 and 12 Cluster:

- Extend understanding of fraction equivalence and ordering
- Understand decimal notation for fractions, and compare decimal fractions


## New Jersey Student Learning Standards (NJSLS)

The Math Practices, as put forth by the National Council of Teachers of Mathematics (NCTM), are connected within all lessons:

MP. 1 - Make sense of problems and persevere in solving them.
MP. 2 - Reason abstractly and quantitatively.

MP. 3 - Construct viable arguments and critique the reasoning of others.
MP. 4 - Model with mathematics.
MP. 5 - Use appropriate tools strategically.
MP. 6 - Attend to precision.
MP. 7 - Look for and make use of structure.
MP. 8 - Look for and express regularity in repeated reasoning.

MA.4.NF
MA.4.NF.A
MA.4.NF.A. 1

MA.4.NF.A. 2

MA.4.NF.B

MA.4.NF.B. 3
MA.4.NF.B. 4

MA.4.NF.B.3a

MA.4.NF.B.3b

MA.4.NF.B.3c

MA.4.NF.B.3d

MA.4.NF.B.4a
MA.4.NF.B.4b

MA.4.NF.B.4c

MA.4.NF.C
MA.4.NF.C. 5

## Number and Operations-Fractions

Extend understanding of fraction equivalence and ordering.
Explain why a fraction $a / b$ is equivalent to a fraction $(n \times a) /(n \times b)$ by using visual fraction models, with attention to how the number and size of the parts differ even though the two fractions themselves are the same size. Use this principle to recognize and generate equivalent fractions.

Compare two fractions with different numerators and different denominators, e.g., by creating common denominators or numerators, or by comparing to a benchmark fraction such as $1 / 2$. Recognize that comparisons are valid only when the two fractions refer to the same whole. Record the results of comparisons with symbols $>,=$, or $<$, and justify the conclusions, e.g., by using a visual fraction model.
Build fractions from unit fractions by applying and extending previous understandings of operations on whole numbers.

Understand a fraction $a / b$ with $a>1$ as a sum of fractions $1 / b$.
Apply and extend previous understandings of multiplication to multiply a fraction by a whole number.

Understand addition and subtraction of fractions as joining and separating parts referring to the same whole.

Decompose a fraction into a sum of fractions with the same denominator in more than one way, recording each decomposition by an equation. Justify decompositions, e.g., by using a visual fraction model.

Add and subtract mixed numbers with like denominators, e.g., by replacing each mixed number with an equivalent fraction, and/or by using properties of operations and the relationship between addition and subtraction.

Solve word problems involving addition and subtraction of fractions referring to the same whole and having like denominators, e.g., by using visual fraction models and equations to represent the problem.

Understand a fraction $a / b$ as a multiple of $1 / b$.
Understand a multiple of $a / b$ as a multiple of $1 / b$, and use this understanding to multiply a fraction by a whole number.

Solve word problems involving multiplication of a fraction by a whole number, e.g., by using visual fraction models and equations to represent the problem.

Understand decimal notation for fractions, and compare decimal fractions.
Express a fraction with denominator 10 as an equivalent fraction with denominator 100, and use this technique to add two fractions with respective denominators 10 and 100.
MA.4.NF.C. 6

Compare two decimals to hundredths by reasoning about their size. Recognize that comparisons are valid only when the two decimals refer to the same whole. Record the results of comparisons with the symbols $>,=$, or <, and justify the conclusions, e.g., by using a visual model.

For example, use a visual fraction model to express $3 \times(2 / 5)$ as $6 \times(1 / 5)$, recognizing this product as 6/5. (In general, $n \times(a / b)=(n \times a) / b$.)

For example, use a visual fraction model to represent $5 / 4$ as the product $5 \times(1 / 4)$, recording the conclusion by the equation $5 / 4=5 \times(1 / 4)$.

For example, express $3 / 10$ as $30 / 100$, and add $3 / 10+4 / 100=34 / 100$.
For example, if each person at a party will eat $3 / 8$ of a pound of roast beef, and there will be 5 people at the party, how many pounds of roast beef will be needed? Between what two whole numbers does your answer lie?
For example, rewrite 0.62 as 62/100; describe a length as 0.62 meters; locate 0.62 on a number line diagram.

## Interdisciplinary Connections

LA.L.4. 4

LA.RF.4.3

LA.RF.4.3.A

LA.RI.4.1

LA.RL.4.1

Determine or clarify the meaning of unknown and multiple-meaning words and phrases based on grade 4 reading and content, choosing flexibly from a range of strategies.

Know and apply grade-level phonics and word analysis skills in decoding and encoding words.

Use combined knowledge of all letter-sound correspondences, syllabication patterns, and morphology (e.g., roots and affixes) to read accurately unfamiliar multisyllabic words in context and out of context.

Refer to details and examples in a text and make relevant connections when explaining what the text says explicitly and when drawing inferences from the text.
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## Learning Objectives

## After completing Unit 3, students will be able to:

## Topic 8:

- Use area models to recognize and generate equivalent fractions.
- Use a number line to locate and identify equivalent fractions.
- Use multiplication to find equivalent fractions.
- Use division to find equivalent fractions.
- Use benchmarks, area models, and number lines to compare fractions.
- Use models or rename fractions to compare.
- Construct arguments about fractions.


## Topic 12:

- Relate fractions and decimals with denominators of 10 and 100.
- Locate and describe fractions and decimals on number lines.
- Compare decimals by reasoning about their size.
- Add fractions with denominators of 10 and 100 by using equivalent fractions.
- Use fractions or decimals to solve word problems involving money.
- Use the structure of the place-value system for decimals to solve problems.


## Suggested Activities \& Best Practices

- Consider Extension Activity e.g. Topic 12-1, pg. 623
- Further suggested activities embedded within each Topic


## Assessment Evidence - Checking for Understanding (CFU)

- Common Formative Assessments (Formative)
- Common Summative Assessments (Summative)
- District Benchmark (Benchmark)
- Do Now
- Exit Tickets
- Higher-order Questioning / Rich Discussion
- Journals
- KWL Chart
- Learning Center Activities
- Performance Task (Alternative)
- Quick Check (enVisionmath)
- Quick Write
- Quizzes (Formative)
- Rubrics
- Surveys
- Teacher Observation Checklist
- Think-Pair-Share
- Turn-and-Talk / Share-out
- Unit Assessments (Summative)
- WIK / WINK

EnVision Math Teacher Edition
PearsonRealize.com

## Ancillary Resources

New Jersey Student Learning Standards for Mathematics
NJSLS Mathematics Crosswalk
IXL Learning
NCTM Illuminations

## Technology Infusion



## Alignment to 21st Century Skills \& Technology

Mastery and infusion of 21st Century Skills \& Technology and their Alignment to the core content areas is essential to student learning. The core content areas include:

- English Language Arts;
- Mathematics;
- Science and Scientific Inquiry (Next Generation);
- Social Studies, including American History, World History, Geography, Government and Civics, and Economics;
- World languages;
- Technology;
- Visual and Performing Arts.

CRP.K-12.CRP2.1

CRP.K-12.CRP4.1

CRP.K-12.CRP6.1

CRP.K-12.CRP8.1

CRP.K-12.CRP11.1

CAEP.9.2.4.A. 4

TECH.8.1.5.A

TECH.8.1.5.A. 1

TECH.8.1.5.A.CS1
TECH.8.1.5.A.CS2

Career-ready individuals readily access and use the knowledge and skills acquired through experience and education to be more productive. They make connections between abstract concepts with real-world applications, and they make correct insights about when it is appropriate to apply the use of an academic skill in a workplace situation.

Career-ready individuals communicate thoughts, ideas, and action plans with clarity, whether using written, verbal, and/or visual methods. They communicate in the workplace with clarity and purpose to make maximum use of their own and others' time. They are excellent writers; they master conventions, word choice, and organization, and use effective tone and presentation skills to articulate ideas. They are skilled at interacting with others; they are active listeners and speak clearly and with purpose. Career-ready individuals think about the audience for their communication and prepare accordingly to ensure the desired outcome.

Career-ready individuals regularly think of ideas that solve problems in new and different ways, and they contribute those ideas in a useful and productive manner to improve their organization. They can consider unconventional ideas and suggestions as solutions to issues, tasks or problems, and they discern which ideas and suggestions will add greatest value. They seek new methods, practices, and ideas from a variety of sources and seek to apply those ideas to their own workplace. They take action on their ideas and understand how to bring innovation to an organization.

Career-ready individuals readily recognize problems in the workplace, understand the nature of the problem, and devise effective plans to solve the problem. They are aware of problems when they occur and take action quickly to address the problem; they thoughtfully investigate the root cause of the problem prior to introducing solutions. They carefully consider the options to solve the problem. Once a solution is agreed upon, they follow through to ensure the problem is solved, whether through their own actions or the actions of others.

Career-ready individuals find and maximize the productive value of existing and new technology to accomplish workplace tasks and solve workplace problems. They are flexible and adaptive in acquiring new technology. They are proficient with ubiquitous technology applications. They understand the inherent risks-personal and organizational-of technology applications, and they take actions to prevent or mitigate these risks.

Explain why knowledge and skills acquired in the elementary grades lay the foundation for future academic and career success.

Technology Operations and Concepts: Students demonstrate a sound understanding of technology concepts, systems and operations.

Select and use the appropriate digital tools and resources to accomplish a variety of tasks including solving problems.

Understand and use technology systems
Select and use applications effectively and productively.

## 21st Century Skills/Interdisciplinary Themes

- Communication and Collaboration
- Creativity and Innovation
- Critical thinking and Problem Solving
- ICT (Information, Communications and Technology) Literacy
- Information Literacy
- Life and Career Skills
- Media Literacy


## 21st Century Skills

- Civic Literacy
- Environmental Literacy
- Financial, Economic, Business and Entrepreneurial Literacy
- Global Awareness
- Health Literacy


## Differentiation

- Use the "Quick Check" feature on Pearson Realize (embedded in each Unit) to help determine the strategy for differentiating instruction; the "Assess and Differentiate" page will prescribe the differentiated instructional activity


## Differentiations:

- Small group instruction
- Small group assignments
- Extra time to complete assignments
- Pairing oral instruction with visuals
- Repeat directions
- Use manipulatives
- Center-based instruction
- Token economy
- Study guides
- Teacher reads assessments aloud
- Scheduled breaks
- Rephrase written directions
- Multisensory approaches
- Additional time
- Preview vocabulary
- Preview content \& concepts
- Story guides
- Behavior management plan
- Highlight text
- Student(s) work with assigned partner
- Visual presentation
- Assistive technology
- Auditory presentations
- Large print edition
- Dictation to scribe


## Hi-Prep Differentiations:

- Alternative formative and summative assessments
- Choice boards
- Games and tournaments
- Group investigations
- Guided Reading
- Independent research and projects
- Interest groups
- Learning contracts
- Leveled rubrics
- Literature circles
- Multiple intelligence options
- Multiple texts
- Personal agendas
- Project-based learning
- Problem-based learning
- Stations/centers
- Think-Tac-Toes
- Tiered activities/assignments
- Tiered products
- Varying organizers for instructions


## Lo-Prep Differentiations

- Choice of books or activities
- Cubing activities
- Exploration by interest
- Flexible grouping
- Goal-setting with students
- Jigsaw
- Mini workshops to re-teach or extend skills
- Open-ended activities
- Think-Pair-Share
- Reading buddies
- Varied journal prompts
- Varied supplemental materials


## Special Education Learning (IEP's \& 504's)

- Consider Intervention Activity and/or Reteach e.g. Topic 12-1, pg. 631A
- Use suggestions under Technology Center section in Pearson Realize to target students with disabilities
- Use the Pacer Center Action Information Sheet for research-based ideas on accommodations and modifications
- Allow for open-note/open-book assessments
- Check classwork frequently for understanding
- Conduct preview of content, concepts, and vocabulary
- Consider behavior management plan
- Implement accommodations/modifications as dictated in the student's IEP/504 plan
- Modified test content/format
- Modified written assignments
- Multi-sensory presentation
- Pre-annotate text
- Preferential seating
- Promote pair work
- Provide extended time on various assignments
- Provide printed/online copies of lesson notes
- Secure attention before providing instruction/directions
- Use assistive technology


## English Language Learning (ELL)

- Use Teaching Tool 48 as a graphic organizer to help students connect a visual to the vocabulary term
- Use Teaching Tool 49 to connect students' understanding of vocabulary terms with actual meanings
- Use suggestions under English Language Learners section in Pearson Realize to target beginning, intermediate, and advanced learners e.g. Topic 12-1, pg. 627A
- Use suggestions under Technology Center section in Pearson Realize to target ELLs
- Allow for multiple student revisions
- Allow for open-note / open-book assessments
- Allow multiple forms of student products (projects, models, slide-shows, etc.) to demonstrate student learning
- Ask and give information using key words
- Demonstrate listening comprehension by responding to questions
- Develop basic sight vocabulary
- Differentiate assessments to reflect selected objectives
- Express ideas in single words
- Leverage computer spell checker
- Modify reading assignments to correlate with lexile level
- Peer tutoring / Peer note-taking
- Speak using content area vocabulary in context
- Teacher-created Study Guide
- Use prior experiences to understanding meanings
- Use videos, illustrations, pictures, and drawings to explain or clarify


## At Risk

- Decrease the amount of work represented or required by assigning the "Do You Understand?" and the "Do You Know How?" sections of each lesson
- Use suggestions under Technology Center section in Pearson Realize to target at-risk students
- Use suggestions under Intervention Activity e.g. Topic 12-1, Error Intervention, pg. 629-630
- Allow for multiple student revisions
- Allow for open-note / open-book assessments
- Allow multiple forms of student products (projects, models, slide-shows, etc.) to demonstrate student learning
- Allow students to select from given assignment choices
- Differentiate assessments to reflect selected objectives
- Mark students' correct and acceptable work, not the mistakes
- Peer tutoring / Peer note-taking
- Promote student collaboration on in-class / outside class assignments
- Reduce lengthy outside reading assignments
- Teach key aspects of a topic - eliminate non-essential information
- Teacher-created Study Guide
- Use authentic assessments with real-life problem-solving
- Use videos, illustrations, pictures, and drawings to explain or clarify


## Talented and Gifted Learning (T\&G)

- Use suggestions under Extension for Early Finishers section in Pearson Realize to target advanced learners
- Use suggestions under Advanced Activity Centers to target advanced learners e.g. Topic 12-1, pg. 631A
- Administer Unit Assessment to determine level of proficiency
- Allow gifted children to create and publish a class newspaper to distribute
- Allow students to work at a faster pace
- Complete activities aligned with above grade-level text using Benchmark results
- Consider parental input about the education of their gifted children
- Create a blog or social media page about a topic of interest
- Create a plan to solve an issue presented in the class or in a text
- Debate issues with research to support arguments
- Involve students in academic contests
- Promote advanced problem-solving
- Remember that gifted children may not excel in all areas
- Set individual goals
- Utilize exploratory connections to higher-grade concepts
- Utilize project-based learning for greater depth of knowledge

