

Unit 4 Systems of Equations and Inequalities

Content Area: **Math**
Course(s): **Algebra 1**
Time Period:
Length: **22 days**
Status: **Published**

Algebra 1

Department of Curriculum and Instruction



Belleville Public Schools

Curriculum Guide

Algebra 1, Grade 8

Unit 4 Systems of Equations and Inequalities

Belleville Board of Education

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Unit Overview

- This unit is about solving and graphing systems of equations and inequalities.
- The students in this unit should learn different methods of solving systems of equations and inequalities, and graph their solution sets on the coordinate plane.

Enduring Understanding

- Interpret and represent system of equations/inequalities to model real-world situation.
- Select a solution from a variety of ways and explain the solution based on this model.
- Make sense of problems and persevere in solving them.
- Reason abstractly and quantitatively.
- Construct viable arguments and critique the reasoning of others.
- Attend to precision.
- Look for and make use of structure.
- Look for and express regularity in repeated reasoning.

Essential Questions

- How can you solve a system of equations or inequalities?
- How do systems of equations model real-world situations?
- What are different methods of solving systems of equations and what are the advantages and disadvantages of each?
- How might you determine which technique for solving a system of equations is appropriate?
- How do you approximate the solution of a system of equations by graphing?
- How can you use the system of equations/inequalities to model and solve contextual problems?

Exit Skills

By the end of Unit 4 Students Should be able to:

- Solve systems of equations by graphing.
- Solving systems of equations using substitution.
- Solving systems of equations using elimination
- Analyze special systems of equations/inequalities (no solution, infinite solutions).
- Solve systems by addition/ subtraction to eliminate a variable.
- Solve systems by multiplication of a row or both rows to eliminate a variable.
- Solve systems of inequalities by graphing.
- Choose the best method of solving a system of linear equations.
- Graph systems of linear inequalities in two variables.
- Explore systems of equations and inequalities, and they find and interpret their solutions.
- Model real-world situations using systems of linear equations/inequalities.

New Jersey Student Learning Standards (NJSL)

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|-----------|--|
| MA.K-12.1 | Make sense of problems and persevere in solving them. |
| MA.K-12.3 | Construct viable arguments and critique the reasoning of others. |
| MA.K-12.4 | Model with mathematics. |

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|---------------|---|
| MA.K-12.5 | Use appropriate tools strategically. |
| MA.K-12.6 | Attend to precision. |
| MA.A-CED.A.2 | Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales. |
| MA.A-CED.A.3 | Represent constraints by equations or inequalities, and by systems of equations and/or inequalities, and interpret solutions as viable or nonviable options in a modeling context. |
| MA.A-REI.C.5 | Prove that, given a system of two equations in two variables, replacing one equation by the sum of that equation and a multiple of the other produces a system with the same solutions. |
| MA.A-REI.C.6 | Solve systems of linear equations exactly and approximately (e.g., with graphs), focusing on pairs of linear equations in two variables. |
| MA.A-REI.C.7 | Solve a simple system consisting of a linear equation and a quadratic equation in two variables algebraically and graphically. |
| MA.A-REI.D.12 | Graph the solutions to a linear inequality in two variables as a half plane (excluding the boundary in the case of a strict inequality), and graph the solution set to a system of linear inequalities in two variables as the intersection of the corresponding half-planes. |

Interdisciplinary Connections

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|-------------|---|
| LA.SL.8.1 | Engage effectively in a range of collaborative discussions (one-on-one, in groups, and teacher-led) with diverse partners on grade 8 topics, texts, and issues, building on others' ideas and expressing their own clearly. |
| LA.SL.8.1.B | Follow rules for collegial discussions and decision-making, track progress toward specific goals and deadlines, and define individual roles as needed. |
| LA.SL.8.1.C | Pose questions that connect the ideas of several speakers and respond to others' questions and comments with relevant evidence, observations, and ideas. |
| LA.SL.8.1.D | Acknowledge new information expressed by others, and, when warranted, qualify or justify their own views in light of the evidence presented. |

Learning Objectives

Students will be able to:

- Solve systems of equations by graphing.
- Analyze special systems of equations/inequalities (no solution, infinite solutions) by their intersections.
- Solve systems of equations using substitution.
- Solve systems by addition/ subtraction to eliminate a variable.
- Solve systems by multiplication of a row or both rows to eliminate a variable
- Choose the best method of solving a system of linear equations.
- Compare different methods of solving systems of inequalities.

- Graph system of equation/inequalities in two variables.
- Manipulate with graphing calculator to analyze set of solutions of systems of equations/inequalities in two variables.
- Model real-world situations using systems of linear equations/inequalities.

| Remember | Understand | Apply | Analyze | Evaluate | Create |
|-----------------|-------------------|--------------|----------------|-----------------|---------------|
| Choose | Classify | Choose | Categorize | Appraise | Combine |
| Describe | Defend | Dramatize | Classify | Judge | Compose |
| Define | Demonstrate | Explain | Compare | Criticize | Construct |
| Label | Distinguish | Generalize | Differentiate | Defend | Design |
| List | Explain | Judge | Distinguish | Compare | Develop |
| Locate | Express | Organize | Identify | Assess | Formulate |
| Match | Extend | Paint | Infer | Conclude | Hypothesize |
| Memorize | Give Examples | Prepare | Point out | Contrast | Invent |
| Name | Illustrate | Produce | Select | Critique | Make |
| Omit | Indicate | Select | Subdivide | Determine | Originate |
| Recite | Interrelate | Show | Survey | Grade | Organize |
| Select | Interpret | Sketch | Arrange | Justify | Plan |
| State | Infer | Solve | Breakdown | Measure | Produce |
| Count | Match | Use | Combine | Rank | Role Play |
| Draw | Paraphrase | Add | Detect | Rate | Drive |
| Outline | Represent | Calculate | Diagram | Support | Devise |
| Point | Restate | Change | Discriminate | Test | Generate |
| Quote | Rewrite | Classify | Illustrate | | Integrate |
| Recall | Select | Complete | Outline | | Prescribe |
| Recognize | Show | Compute | Point out | | Propose |
| Repeat | Summarize | Discover | Separate | | Reconstruct |
| Reproduce | Tell | Divide | | | Revise |
| | Translate | Examine | | | Rewrite |
| | Associate | Graph | | | Transform |
| | Compute | Interpolate | | | |
| | Convert | Manipulate | | | |
| | Discuss | Modify | | | |
| | Estimate | Operate | | | |
| | Extrapolate | Subtract | | | |
| | Generalize | | | | |
| | Predict | | | | |



Suggested Activities & Best Practices

System of Equations - Elimination:

<https://whenmathhappens.com/2015/10/15/elimination-50min/>

System of Equations - Substitution:

<https://whenmathhappens.com/2015/10/15/submethod-50min/>

<http://mathbitsnotebook.com/Algebra1/Systems/SYoutline.html>

Real-World Applications of System of Equations:

<https://betterlesson.com/lesson/427886/real-life-systems-3-easy-price?from=search>

<https://tapintoteenminds.com/3act-math/counting-candy-sequel/>

<https://teacher.desmos.com/activitybuilder/custom/5670acf05a543a6007737ea8>

<https://teacher.desmos.com/activitybuilder/custom/5818fb314e762b653c3bf0f3>

<https://www.yummymath.com/2013/souvenirs-and-concessions-2/>

System of Equations, flashcard, notes, examples, practice

<https://quizlet.com/subject/system-of-equations/>

Textbook, eAssessment, supplemental materials:

<https://my.mheducation.com/login>

AI Assessment and Learning System:

<https://www.aleks.com/>

Mindset:

<https://www.youtube.com/watch?v=3icoSeGqQtY>

<http://www.youcubed.org/wp-content/uploads/Positive-Classroom-Norms2.pdf>

Teaching Strategies for Improving Algebra Knowledge in Middle and High School Students:

<https://ies.ed.gov/ncee/wwc/PracticeGuide/20>

Coaching Corner:

<https://sites.google.com/belleville.k12.nj.us/thecoachingcorner/home>

Algebra Tools - Functions:

<https://www.state.nj.us/education/aps/cccs/math/NJISTFunctions.pdf>

Algebra Tools - Algebra:

<https://www.state.nj.us/education/aps/cccs/math/NJISTAAlgebra.pdf>

Misc Mathematics materials:

<http://www.mathnstuff.com/>

Algebra Kahoots:

<https://kahoot.com/explore/collections/math-kahoot-algebra/>

Assessment Evidence - Checking for Understanding (CFU)

- Solving Systems of Equations by Graphing <https://create.kahoot.it/details/systems-of-equations-graphing/36a34bb9-d049-4cea-b9ee-d2ef426b31d0> (formative assessment)
- Homework (formative assessment)
- Benchmark #3 (summative assessment)

- Creating and solving a study guide (alternative assessment)
 - Take home quizzes (alternative assessments)
 - Do Nows (formative assessments)
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- Admit Tickets
 - Anticipation Guide
 - Common Benchmarks
 - Compare & Contrast
 - Describe
 - Evaluate
 - Evaluation rubrics
 - Exit Tickets
 - Explaining
 - Fist- to-Five or Thumb-Ometer
 - Illustration
 - Journals
 - KWL Chart
 - Learning Center Activities
 - Multimedia Reports
 - Quizzes
 - Red Light, Green Light
 - Study Guide
 - Teacher Observation Checklist
 - Think, Pair, Share
 - Unit review/Test prep
 - Unit tests

Primary Resources & Materials

Glencoe McGraw-Hill Algebra1 2014

Glencoe McGraw-Hill Algebra1 2010

Practice Glencoe Algebra1

Study Guide Glencoe Algebra1

Ancillary Resources

Glencoe Algebra 1 Tutor: Personal Tutor and Spanish Tutor

Glencoe Algebra 1 Geometer's Sketchpad

Glencoe Algebra 1 Glencoe Mathematics Secondary Series

ALEKS

Technology Infusion

- Kahoot <https://create.kahoot.it/details/b83429c3-489f-4232-8ca6-c3c996131c63>
- Youtube
- Khan academy
- Edulastic
- Google Sheets
- Google Classroom
- Office 365
- Google Docs
- PodCasts
- Google Slides
- Wikipedia
- Skype
- Twitter
- Ted Talks
- QR Barcode Generator
- Calculator/Graphic calculator
- desmos.com
- geogebra.org

Win 8.1 Apps/Tools Pedagogy Wheel

Originally taken from <http://www.coetail.com/vzimmer/files/2013/02/iPadagogy-Wheel.001.jpg>
And adapted for Windows 8.1 devices by Charlotte Beckhurst @CharBeckhurst



Alignment to 21st Century Skills & Technology

- English, reading or language arts
- Economics
- Science

- Geography
- History
- Government and Civics

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|-------------------|--|
| CRP.K-12.CRP2 | Apply appropriate academic and technical skills. |
| CRP.K-12.CRP4 | Communicate clearly and effectively and with reason. |
| CRP.K-12.CRP7 | Employ valid and reliable research strategies. |
| CRP.K-12.CRP8 | Utilize critical thinking to make sense of problems and persevere in solving them. |
| CRP.K-12.CRP11 | Use technology to enhance productivity. |
| CAEP.9.2.12.C.2 | Modify Personalized Student Learning Plans to support declared career goals. |
| TECH.8.1.12.A.3 | Collaborate in online courses, learning communities, social networks or virtual worlds to discuss a resolution to a problem or issue. |
| TECH.8.1.12.F.1 | Evaluate the strengths and limitations of emerging technologies and their impact on educational, career, personal and or social needs. |
| TECH.8.2.12.D.CS2 | Use and maintain technological products and systems. |

21st Century Skills/Interdisciplinary Themes

- Communication and Collaboration
- Creativity and Innovation
- Critical thinking and Problem Solving
- ICT (Information, Communications and Technology) Literacy

21st Century Skills

- Civic Literacy
- Financial, Economic, Business and Entrepreneurial Literacy
- Health Literacy

Differentiation

- Use of larger version of coordinate plane to graph systems of equations
- Color coding each equation in the system of equations
- Graphic organizer with steps to solving systems of equations utilized in multiple methods

- Use of graphing calculator TI 84 to graph and solve system of equations
- Cooperative groups
- Pairing oral instruction with visuals
- Team work
- Center based instruction
- Repeat directions as needed
- Study guide
- Tests/quizzes reviews
- Notes taking/transparencies
- Organizer
- Calculator/graphing calculator
- Extra time
- Students work with assigned partner
- Choice boards
- Stations/Learning centers

Special Education Learning (IEP's & 504's)

- Use of larger version of coordinate plane to graph systems of equation
 - Color coding each equation in the system of equations
 - Graphic organizer with steps to solving systems of equations utilized in multiple methods
 - Use of graphing calculator TI 84 to graph and solve system of equations
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- printed copy of board work/notes provided
 - additional time for skill mastery
 - assistive technology
 - Center-Based Instruction
 - check work frequently for understanding
 - computer or electronic device utilizes
 - extended time on tests/ quizzes
 - have student repeat directions to check for understanding
 - highlighted text visual presentation
 - modified assignment format
 - modified test content
 - modified test format
 - modified test length
 - preferential seating
 - preview of content, concepts, and vocabulary
 - Provide modifications as dictated in the student's IEP/504 plan
 - secure attention before giving instruction/directions
 - shortened assignments

- student working with an assigned partner
- Use open book, study guides, test prototypes

English Language Learning (ELL)

- Use of larger version of coordinate plane to graph systems of equations
 - Color coding each equation in the system of equations
 - Graphic organizer with steps to solving systems of equations utilized in multiple methods
 - Use of graphing calculator TI 84 to graph and solve system of equations
-
- teaching key aspects of a topic. Eliminate nonessential information
 - using videos, illustrations, pictures, and drawings to explain or clarify
 - allowing products (projects, timelines, demonstrations, models, drawings, dioramas, poster boards, charts, graphs, slide shows, videos, etc.) to demonstrate student's learning;
 - allowing students to correct errors (looking for understanding)
 - allowing the use of note cards or open-book during testing
 - decreasing the amount of work presented or required
 - having peers take notes or providing a copy of the teacher's notes
 - modifying tests to reflect selected objectives
 - providing study guides
 - reducing or omitting lengthy outside reading assignments
 - reducing the number of answer choices on a multiple choice test
 - tutoring by peers

At Risk

- Use of larger version of coordinate plane to graph systems of equations
 - Color coding each equation in the system of equations
 - Graphic organizer with steps to solving systems of equations utilized in multiple methods
 - Use of graphing calculator TI 84 to graph and solve system of equations
-
- allowing students to correct errors (looking for understanding)
 - teaching key aspects of a topic. Eliminate nonessential information
 - allowing products (projects, timelines, demonstrations, models, drawings, dioramas, poster boards, charts, graphs, slide shows, videos, etc.) to demonstrate student's learning
 - allowing students to select from given choices
 - allowing the use of note cards or open-book during testing
 - collaborating (general education teacher and specialist) to modify vocabulary, omit or modify items to reflect objectives for the student, eliminate sections of the test, and determine how the grade will be determined prior to giving the test.

- decreasing the amount of work presented or required
- having peers take notes or providing a copy of the teacher's notes
- marking students' correct and acceptable work, not the mistakes
- modifying tests to reflect selected objectives
- providing study guides
- reducing the number of answer choices on a multiple choice test
- tutoring by peers
- using authentic assessments with real-life problem-solving
- using videos, illustrations, pictures, and drawings to explain or clarify

Talented and Gifted Learning (T&G)

- Solving System of Equations in Context <https://tapintoteenminds.com/3act-math/counting-candy-sequel/>

- Above grade level placement option for qualified students
- Advanced problem-solving
- Allow students to work at a faster pace
- Complete activities aligned with above grade level text using Benchmark results
- Flexible skill grouping within a class or across grade level for rigor
- Higher order, critical & creative thinking skills, and discovery
- Multi-disciplinary unit and/or project
- Teacher-selected instructional strategies that are focused to provide challenge, engagement, and growth opportunities
- Utilize exploratory connections to higher-grade concepts

Sample Lesson

Using the template below, please develop a **Sample Lesson** for the first unit only.

Unit Name:

NJSLS:

Interdisciplinary Connection:

Statement of Objective:

Anticipatory Set/Do Now:

Learning Activity:

Student Assessment/CFU's:

Materials:

21st Century Themes and Skills:

Differentiation/Modifications:

Integration of Technology: