Unit 1 Limits

What role do limits play in calculus?

Content Area: Course(s): Time Period: Length: Status:	Mathematics Calculus Honors Marking Period 1 10 Blocks Published	
Transfer Skills Limits: Taking it to the Limits		
	students will evaluate limits numerically, graphically, and analytically as a means of from Pre-Calculus procedures to the Calculus process of differentiation.	
	Understandings	
The concept	of limits is one of the foundations of calculus.	
The concept	of limits can be applied throughout mathematics.	
Essential (
What does the	ne slope of a line represent?	
What is calc	ulus?	
What is a lin	nit?	
When does a	a limit not exist?	

How are limits and continuity related?		
Content		
Notes:		
* Begin with describing the tangent line and rates of change problems as the big ideas for this unit		
* A conceptual look at limits using graphs is helpful before your begin calculating them		
* Properties of limits are sum/difference, product/quotient, scalar multiplication, limits raised to an exponent, limit of a constant		
* Trig limits are generally a weak point here		
Vocabulary		
average rate of change		
secant line		
instantaneous rate of change		
tangent line		
limits		
continutity		
Intermediate Value Theorem		
Skills Find the average rate of change of a function over an interval		
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Determine the slope of a secant line through a curve
Define the instantaneous rate of change of a function at a given point
Write the equation of a tangent line
Find the slope of a curve at a point using a table
Determine the value of one and two sided limits using a table and a graph
Use properties of limits to evaluate limits
Evaluate limits algebraically using cancelation, rationalization, and special trigonometric limits
Evaluate limits approaching infinity
Relate limits to continutity
Use the Intermediate Value Theorem to verify function values
Resources
Text:
James Stewart Calculus Eighth Edition
Graphing Calculator
Online Resources:
Khan Academy

Geogebra
Desmos
Standards
NJSLS 2016
Arithmetic with Polynomials and Rational Expressions
A -APR A. Perform arithmetic operations on polynomials
B. Understand the relationship between zeros and factors of polynomials
3. Identify zeros of polynomials when suitable factorizations are available, and use the zeros to construct a rough graph of the function defined by the polynomial.
Seeing Structure in Expressions
A-SSE B. Write expressions in equivalent forms to solve problems
3. Choose and produce an equivalent form of an expression to reveal and explain properties of the quantity represented by the expression. ★
a. Factor a quadratic expression to reveal the zeros of the function it defines.
Interpreting Functions
F-IF A. Understand the concept of a function and use function

- 1. Understand that a function from one set (called the domain) to another set (called the range) assigns to each element of the domain exactly one element of the range. If f is a function and x is an element of its domain, then f(x) denotes the output of f corresponding to the input x. The graph of f is the graph of the equation y = f(x).
- 2. Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context.

B. Interpret functions that arise in applications in terms of the context

5. Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes. For example, if the function h(n) gives the number of person-hours it takes to assemble n engines in a factory, then the positive integers would be an appropriate domain for the function.

Mathematics | Standards for Mathematical Practice

1 Make sense of problems and persevere in solving them.

Mathematically proficient students start by explaining to themselves the meaning of a problem and looking for entry points to its solution. They analyze givens, constraints, relationships, and goals. They make conjectures about the form and meaning of the solution and plan a solution pathway rather than simply jumping into a solution attempt. They consider analogous problems, and try special cases and simpler forms of the original problem in order to gain insight into its solution. They monitor and evaluate their progress and change course if necessary. Older students might, depending on the context of the problem, transform algebraic expressions or change the viewing window on their graphing calculator to get the information they need. Mathematically proficient students can explain correspondences between equations, verbal descriptions, tables, and graphs or draw diagrams of important features and relationships, graph data, and search for regularity or trends. Younger students might rely on using concrete objects or pictures to help conceptualize and solve a problem. Mathematically proficient students check their answers to problems using a different method, and they continually ask themselves, "Does this make sense?" They can understand the approaches of others to solving complex problems and identify correspondences between different approaches.

2 Reason abstractly and quantitatively.

Mathematically proficient students make sense of quantities and their relationships in problem situations. They bring two complementary abilities to bear on problems involving quantitative relationships: the ability to decontextualize—to abstract a given situation and represent it symbolically and manipulate the representing symbols as if they have a life of their own, without necessarily attending to their referents—and the ability to contextualize, to pause as needed during the manipulation process in order to probe into the referents for the

symbols involved. Quantitative reasoning entails habits of creating a coherent representation of the problem at hand; considering the units involved; attending to the meaning of quantities, not just how to compute them; and knowing and flexibly using different properties of operations and objects.

5 Use appropriate tools strategically.

Mathematically proficient students consider the available tools when solving a mathematical problem. These tools might include pencil and paper, concrete models, a ruler, a protractor, a calculator, a spreadsheet, a computer algebra system, a statistical package, or dynamic geometry software. Proficient students are sufficiently familiar with tools appropriate for their grade or course to make sound decisions about when each of these tools might be helpful, recognizing both the insight to be gained and their limitations. For example, mathematically proficient high school students analyze graphs of functions and solutions generated using a graphing calculator. They detect possible errors by strategically using estimation and other mathematical knowledge. When making mathematical models, they know that technology can enable them to visualize the results of varying assumptions, explore consequences, and compare predictions with data. Mathematically proficient students at various grade levels are able to identify relevant external mathematical resources, such as digital content located on a website, and use them to pose or solve problems. They are able to use technological tools to explore and deepen their understanding of concepts.

6 Attend to precision.

Mathematically proficient students try to communicate precisely to others. They try to use clear definitions in discussion with others and in their own reasoning. They state the meaning of the symbols they choose, including using the equal sign consistently and appropriately. They are careful about specifying units of measure, and labeling axes to clarify the correspondence with quantities in a problem. They calculate accurately and efficiently, express numerical answers with a degree of precision appropriate for the problem context. In the elementary grades, students give carefully formulated explanations to each other. By the time they reach high school they have learned to examine claims and make explicit use of definitions.

CCSS.Math.Practice.MP1 Make sense of problems and persevere in solving them.

CCSS.Math.Content.HSF-IF Interpreting Functions

CCSS.Math.Content.HSA-SSE Seeing Structure in Expressions

CCSS.Math.Content.HSF-IF.A Understand the concept of a function and use function notation

Mathematically proficient students start by explaining to themselves the meaning of a problem and looking for entry points to its solution. They analyze givens, constraints,

relationships, and goals. They make conjectures about the form and meaning of the solution and plan a solution pathway rather than simply jumping into a solution attempt. They consider analogous problems, and try special cases and simpler forms of the original problem in order to gain insight into its solution. They monitor and evaluate their progress and change course if necessary. Older students might, depending on the context of the problem, transform algebraic expressions or change the viewing window on their graphing calculator to get the information they need. Mathematically proficient students can explain correspondences between equations, verbal descriptions, tables, and graphs or draw diagrams of important features and relationships, graph data, and search for regularity or trends. Younger students might rely on using concrete objects or pictures to help conceptualize and solve a problem. Mathematically proficient students check their answers to problems using a different method, and they continually ask themselves, "Does this make sense?" They can understand the approaches of others to solving complex problems and identify correspondences between different approaches.

CCSS.Math.Content.HSF-IF.A.1

Understand that a function from one set (called the domain) to another set (called the range) assigns to each element of the domain exactly one element of the range. If f is a function and x is an element of its domain, then f(x) denotes the output of f corresponding to the input x. The graph of f is the graph of the equation y = f(x).

CCSS.Math.Practice.MP2

Reason abstractly and quantitatively.

CCSS.Math.Content.HSF-IF.A.2

Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context.

Mathematically proficient students make sense of quantities and their relationships in problem situations. They bring two complementary abilities to bear on problems involving quantitative relationships: the ability to decontextualize-to abstract a given situation and represent it symbolically and manipulate the representing symbols as if they have a life of their own, without necessarily attending to their referents-and the ability to contextualize, to pause as needed during the manipulation process in order to probe into the referents for the symbols involved. Quantitative reasoning entails habits of creating a coherent representation of the problem at hand; considering the units involved; attending to the meaning of quantities, not just how to compute them; and knowing and flexibly using different properties of operations and objects.

CCSS.Math.Content.HSF-IF.B

Interpret functions that arise in applications in terms of the context

CCSS.Math.Practice.MP5

Use appropriate tools strategically.

CCSS.Math.Content.HSA-SSE.B

Write expressions in equivalent forms to solve problems

CCSS.Math.Content.HSF-IF.B.5 Relate the c

Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes.

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CCSS.Math.Content.HSA-SSE.B.3.a

Factor a quadratic expression to reveal the zeros of the function it defines.

CCSS.Math.Practice.MP6

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MA.A-APR Arithmetic with Polynomials and Rational Expressions

CCSS.Math.Content.HSA-APR Arithmetic with Polynomials and Rational Expressions

MA.A-APR.A Perform arithmetic operations on polynomials

MA.A-APR.B Understand the relationship between zeros and factors of polynomials

CCSS.Math.Content.HSA-APR.B Understand the relationship between zeros and factors of polynomials

CCSS.Math.Content.HSA-APR.B.3 Identify zeros of polynomials when suitable factorizations are available, and use the zeros

to construct a rough graph of the function defined by the polynomial.