# \*Unit 7 Trigonometry (8)

Content Area: Mathematics

Course(s): Integrated Modern Algebra

Time Period: February
Length: 7 blocks
Status: Published

#### **Transfer Skills**

<u>Previous coursework</u>: explain a proof of the pythagorean theorem and its converse, apply the pythagorean theorem

By the end of this unit: Students should understand what a trig ratio is; what does it mean when we say "sin 32°"? They should focus on patterns and relationships with basic co-functions and complementary angles and problems should be solved using any of the six trig functions. Because they will be graphing trig functions in Algebra 2, they should be able to derive the sine and cosine of a 30, 45, and 60 degree angle easily. Honors students extend this knowledge to oblique triangles using Law of Sines and Cosines and the unit circle. The honors student should be able to quickly calculate any trig value on the unit circle given an angle with a 30, 45, or 60 degree reference angle. They should be able to do this with both degree or radian measures less than one rotation (between 0 and 360/2pi).

### <u>Instructional strategies</u>:

- Students have a hard time labeling side lengths- highlight the reference angle in some way to help.
- All six trig functions should be used to solve a right triangle.
- Introduce students to the Unit Circle

# **Enduring Understandings**

Trigonometry uses properties of similar right triangles to determine common ratios between side lengths and acute angle measures.

Trigonometry can find lengths and angles given limited information.

## **Essential Questions**

How is trigonometry related to similar right triangles?

| How can trigonometry be used in real life?   |
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| How does the unit circle relate to the trigonometric functions?  |
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| Content  |
| Special Right Triangles  |
| Finding Sides and Angles using Trigonometric Ratios  |
| The Pythagorean Theorem  |
| Applications of Trigonometry   |
| Radian Measure   |
| Introduction to the Unit Circle  |
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| Skills 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1   |
| Label a triangle in relation to the reference angle (opposite, adjacent & hypotenuse).   |
| Determine the most appropriate trigonometric ratio (sine, cosine, tangent) to use for a given problem based on the information provided. |
| ·  |
| Solve for sides and angles of right triangles using trigonometry.  |
| Explain why similar triangles have the same trigonometric ratio values.  |
| Determine the exact value of the trigonometric ratios for 30, 45, and 60 degree angles.  |

| Explain and use the relationship between the sine and cosine of complementary angles.   |
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| Define radian measure as the length of the arc on the unit circle subtended by the angle.   |
| Write angles in both degrees and radians.   |
| Construct the unit circle from special right triangles.   |
| Calculate exact values for sine, cosine, tangent trigonometric ratios for any radian or degree measure around the unit circle.  |
| Explain how the unit circle in the coordinate plane enables the extension of trigonometric functions to all real numbers, interpreted as radian measures of angles traversed counterclockwise around the unit circle. |
| Sketch an angle given in radians and degrees. Determine an angle measure in radians and degrees from a picture.   |
| Use the relationship of the six trigonometric functions to a central angle of the unit circle to determine the exact trigonometric ratio of angles on the unit circle. (0° to 360°, 0 to 2pi)                         |
| Identify the angle that produce an exact value of a trigonometric function.   |
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| Resources   |
| <u>KhanAcademy</u>  |

| YouTube Website for ALL Math Concepts from Arithmetic to Calculus |
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| www.youtube.com/user/bullcleo1                                    |
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| Math IXL  |
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|   |
| Standards   |
| NJSLS 2016  |
|   |

**HSG-SRT B. Prove theorems involving similarity** 

Similarity, Right Triangles, and Trigonometry

5. Use congruence and similarity criteria for triangles to solve problems and to prove relationships in geometric figures.

#### HSG-SRT C. Define trigonometric ratios and solve problems involving right triangles

- 6. Understand that by similarity, side ratios in right triangles are properties of the angles in the triangle, leading to definitions of trigonometric ratios for acute angles.
- 7. Explain and use the relationship between the sine and cosine of complementary angles.
- 8. Use trigonometric ratios and the Pythagorean Theorem to solve right triangles in applied problems.

#### **Mathematics I Standards for Mathematical Practice**

#### 1 Make sense of problems and persevere in solving them.

Mathematically proficient students start by explaining to themselves the meaning of a problem and looking for entry points to its solution. They analyze givens, constraints, relationships, and goals. They make conjectures about the form and meaning of the solution and plan a solution pathway rather than simply jumping into a solution attempt. They consider analogous problems, and try special cases and simpler forms of the original problem in order to gain insight into its solution. They monitor and evaluate their progress and change course if necessary. Older students might, depending on the context of the problem, transform algebraic expressions or change the viewing window on their graphing calculator to get the information they need. Mathematically proficient students can explain correspondences between equations, verbal descriptions, tables, and graphs or draw diagrams of important features and relationships, graph data, and search for regularity or trends. Younger

students might rely on using concrete objects or pictures to help conceptualize and solve a problem. Mathematically proficient students check their answers to problems using a different method, and they continually ask themselves, "Does this make sense?" They can understand the approaches of others to solving complex problems and identify correspondences between different approaches.

#### 2 Reason abstractly and quantitatively.

Mathematically proficient students make sense of quantities and their relationships in problem situations. They bring two complementary abilities to bear on problems involving quantitative relationships: the ability to decontextualize—to abstract a given situation and represent it symbolically and manipulate the representing symbols as if they have a life of their own, without necessarily attending to their referents—and the ability to contextualize, to pause as needed during the manipulation process in order to probe into the referents for the symbols involved. Quantitative reasoning entails habits of creating a coherent representation of the problem at hand; considering the units involved; attending to the meaning of quantities, not just how to compute them; and knowing and flexibly using different properties of operations and objects.

#### 4 Model with mathematics.

Mathematically proficient students can apply the mathematics they know to solve problems arising in everyday life, society, and the workplace. In early grades, this might be as simple as writing an addition equation to describe a situation. In middle grades, a student might apply proportional reasoning to plan a school event or analyze a problem in the community. By high school, a student might use geometry to solve a design problem or use a function to describe how one quantity of interest depends on another. Mathematically proficient students who can apply what they know are comfortable making assumptions and approximations to simplify a complicated situation, realizing that these may need revision later. They are able to identify important quantities in a practical situation and map their relationships using such tools as diagrams, two-way tables, graphs, flowcharts and formulas. They can analyze those relationships mathematically to draw conclusions. They routinely interpret their mathematical results in the context of the situation and reflect on whether the results make sense, possibly improving the model if it has not served its purpose.

#### 7 Look for and make use of structure.

Mathematically proficient students look closely to discern a pattern or structure. Young students, for example, might notice that three and seven more is the same amount as seven and three more, or they may sort a collection of shapes according to how many sides the shapes have. Later, students will see  $7 \times 8$  equals the well remembered  $7 \times 5 + 7 \times 3$ , in preparation for learning about the distributive property. In the expression  $x^2 + 9x + 14$ , older students can see the 14 as  $2 \times 7$  and the 9 as 2 + 7. They recognize the significance of an existing line in a geometric figure and can use the strategy of drawing an auxiliary line for solving problems. They also can step back for an overview and shift perspective. They can see complicated things, such as some algebraic expressions, as single objects or as being composed of several objects. For example, they can see 5 - 3(x - y) 2 as 5 minus a positive number times a square and use that to realize that its value cannot be more than 5 for any real numbers x and y.

MA.K-12.1

Make sense of problems and persevere in solving them.

MA.K-12.2

Reason abstractly and quantitatively.

MA.K-12.4 Model with mathematics.

MA.G-SRT.C.8

MA.K-12.7 Look for and make use of structure.

MA.G-SRT Similarity, Right Triangles, and Trigonometry

MA.G-SRT.B Prove theorems involving similarity

MA.G-SRT.B.5 Use congruence and similarity criteria for triangles to solve problems and to prove

relationships in geometric figures.

MA.G-SRT.C Define trigonometric ratios and solve problems involving right triangles

MA.G-SRT.C.6 Understand that by similarity, side ratios in right triangles are properties of the angles in

the triangle, leading to definitions of trigonometric ratios for acute angles.

MA.G-SRT.C.7 Explain and use the relationship between the sine and cosine of complementary angles.

Use trigonometric ratios and the Pythagorean Theorem to solve right triangles in applied

problems.

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