

Student: _____
Date: _____

Instructor: Allison Amico
Course: Algebra II

Assignment: MPA-4 2017

I pledge that I will not use any notes, text, or other reference materials during this assignment. I pledge that I will neither give nor receive any aid from any other person during this assignment, and that the work presented here is entirely my own.

Signature _____

Date _____

1. Solve the rational equation. If the equation has no solution, so state.

$$\frac{5}{x-5} - \frac{7}{x-1} = \frac{20}{x^2 - 6x + 5}$$

Select the correct choice below and, if necessary, fill in the answer box within your choice.

- ☐ A. $x =$ _____ (Use a comma to separate answers as needed.)
☐ B. There is no solution.

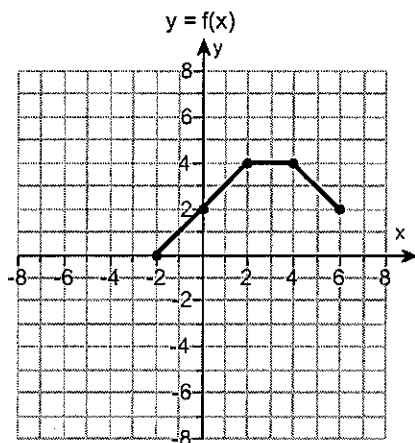
2. Solve the equation.

$$\frac{4}{y} + \frac{3}{4} = \frac{7}{4y}$$

Select the correct answer below and, if necessary, fill in the answer box to complete your choice.

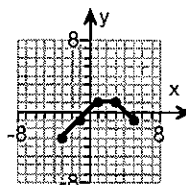
- ☐ A. $y =$ _____ (Use a comma to separate answers if needed.)
☐ B. There is no solution.

- *3. Use the graph of $y = f(x)$ to graph the function $g(x) = f(x - 1) + 3$.

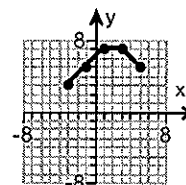


Choose the correct graph of g below.

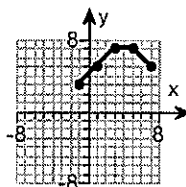
☐ A.



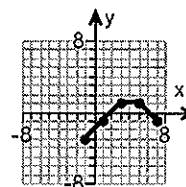
☐ B.



☐ C.



☐ D.



4. Find the value of each variable.

$$\begin{bmatrix} 12 & 6 \\ 16 & 7.5 \end{bmatrix} = \begin{bmatrix} 4x - 4 & 7 - 10t \\ 4x & 15t + 1.5x \end{bmatrix}$$

$x =$ _____ (Simplify your answer. Type an integer or a decimal.)

$t =$ _____ (Simplify your answer. Type an integer or a decimal.)

5. Solve the following equation. Check your solution.

$$\frac{5}{x+1} = \frac{x+2}{x+1}$$

Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

- ☐ A. $x =$ _____ (Simplify your answer. Use a comma to separate answers as needed.)
☐ B. No solution

6. Write the expression shown below in radical form.

$$x^{\frac{1}{5}}$$

$$x^{\frac{1}{5}} =$$

(Simplify your answer, including any radicals. Use integers or fractions for any numbers in the expression.)

7. Find the following product.

$$\begin{bmatrix} -3 & -2 \\ -6 & -1 \end{bmatrix} \begin{bmatrix} 5 & 2 \\ 6 & 6 \end{bmatrix}$$

Select the correct choice below and, if necessary, fill in the answer boxes within your choice.

- ☐ A. The product is $\begin{bmatrix} \underline{\hspace{2cm}} & \underline{\hspace{2cm}} \\ \underline{\hspace{2cm}} & \underline{\hspace{2cm}} \end{bmatrix}$. (Simplify your answers.)
☐ B. The product is not defined.

8. Simplify the expression shown below.

$$\sqrt{3}(\sqrt[6]{3})$$

$$\sqrt{3}(\sqrt[6]{3}) =$$

(Simplify your answer, including any radicals. Use integers or fractions for any numbers in the expression.)

9. Solve.

$$z + \frac{3}{z} = -4$$

Select the correct choice below and, if necessary, fill in the answer box within your choice.

- ☐ A. The solution is $z =$ _____. (Use a comma to separate answers as needed.)
- ☐ B. There is no solution.

10. Solve the equation.

$$\frac{4r-4}{r^2+4r-21} + \frac{4}{r+7} = \frac{2}{r-3}$$

Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

- ☐ A. $r =$ _____
(Type an integer or a simplified fraction. Use a comma to separate answers as needed.)
- ☐ B. There is no solution.

11. Use synthetic division and the given factor to completely factor the polynomial function.

$$x^3 + 8x^2 + 4x - 48; x + 6$$

$$x^3 + 8x^2 + 4x - 48 = (x + 6) \underline{\hspace{2cm}} \text{ (Factor completely.)}$$

12. Find the product $5C$.

$$C = \begin{bmatrix} 2 & -9 \\ 2 & 4 \end{bmatrix}$$

Select the correct choice below and, if necessary, fill in the answer boxes within your choice.

- ☐ A. $5C = \begin{bmatrix} \underline{\hspace{2cm}} & \underline{\hspace{2cm}} \\ \underline{\hspace{2cm}} & \underline{\hspace{2cm}} \end{bmatrix}$ (Simplify your answers.)
- ☐ B. The product is not defined.

13. Solve the equation. Check each solution.

$$\frac{y}{2} + \frac{y}{3} = 5$$

Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

- ☐ A. The solution is $y =$ _____.
(Type an integer or a simplified fraction. Use a comma to separate answers as needed.)
- ☐ B. There are infinitely many solutions.
- ☐ C. There is no solution.

14.

The optimal height h of the letters of a message printed on pavement is given by the formula $h = \frac{0.00252d^{2.27}}{e}$. Here d is the distance of the driver from the letters and e is the height of the driver's eye above the pavement. All of the distances are in meters. Find h for the given values of d and e .

$$d = 91.8 \text{ m} \quad e = 1.4 \text{ m}$$

$$h \approx \underline{\hspace{2cm}} \text{ m}$$

(Round to the nearest tenth as needed.)

15. Solve the matrix equation.

$$X - \begin{bmatrix} 3 & 2 \\ -5 & 2 \end{bmatrix} = \begin{bmatrix} 4 & -4 \\ 2 & 0 \end{bmatrix}$$

$$X = \begin{bmatrix} \underline{\hspace{2cm}} & \underline{\hspace{2cm}} \\ \underline{\hspace{2cm}} & \underline{\hspace{2cm}} \end{bmatrix}$$

16. Divide using long division. Check your answer.

$$(3x^2 - 4x + 5) \div (x - 2)$$

The quotient is $\underline{\hspace{2cm}}$ with remainder $\underline{\hspace{2cm}}$.

17. Use synthetic division and the Remainder Theorem to find $P(a)$.

$$P(x) = 3x^3 - x^2 + 9x + 3; \quad a = \frac{1}{3}$$

$$P\left(\frac{1}{3}\right) = \underline{\hspace{2cm}} \quad (\text{Simplify your answer. Type an integer or a fraction.})$$

18. Find the product of the following matrices, if possible.

$$\begin{bmatrix} -8 & 8 & 2 \\ -8 & -8 & -2 \end{bmatrix} \begin{bmatrix} -6 \\ -5 \\ -7 \end{bmatrix}$$

Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

☐ **A.** $\begin{bmatrix} -8 & 8 & 2 \\ -8 & -8 & -2 \end{bmatrix} \begin{bmatrix} -6 \\ -5 \\ -7 \end{bmatrix} = \begin{bmatrix} \underline{\hspace{2cm}} \\ \underline{\hspace{2cm}} \end{bmatrix}$

☐ **B.** The product is not possible.

19. Find $2A + 3B$.

$$A = \begin{bmatrix} 7 & 9 \\ 4 & 1 \end{bmatrix} \quad B = \begin{bmatrix} -1 & 4 \\ 9 & -8 \end{bmatrix}$$

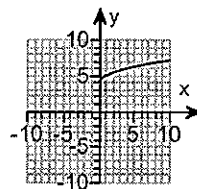
$$2A + 3B = \begin{bmatrix} \underline{\hspace{2cm}} & \underline{\hspace{2cm}} \\ \underline{\hspace{2cm}} & \underline{\hspace{2cm}} \end{bmatrix}$$

*20. Use transformations of $f(x) = \sqrt{x}$ to graph the following function.

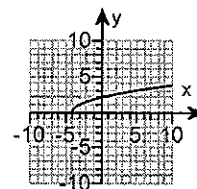
$$g(x) = \sqrt{x} - 4$$

Choose the correct graph below.

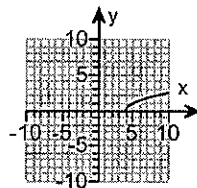
☐ A.



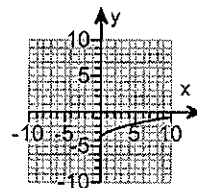
☐ B.



☐ C.



☐ D.



21. Rewrite the expression with rational exponents.

$$\sqrt[4]{x^5}$$

$$\sqrt[4]{x^5} = \underline{\hspace{2cm}}$$

22. Use synthetic division and the remainder theorem to find $P(a)$.

$$P(x) = x^3 + 4x^2 - 5x + 1; a = 4$$

$$P(a) = \underline{\hspace{2cm}}$$

(Simplify your answer.)

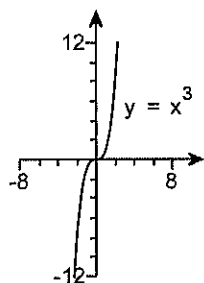
23. Divide using synthetic division.

$$(x^4 - 6x^2 - 26) \div (x + 2)$$

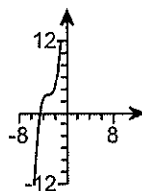
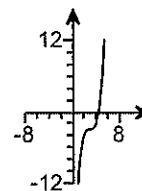
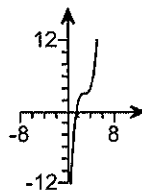
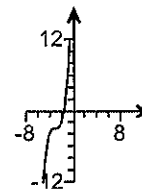
The quotient is $\underline{\hspace{2cm}}$ and the remainder is $\underline{\hspace{2cm}}$.
(Simplify your answers. Do not factor.)

- *24. Graph the function using the techniques of shifting, compressing, stretching, and/or reflecting. Start with the graph of the basic function shown below.

$$f(x) = (x - 3)^3 + 3$$



Choose the correct graph of $f(x)$.

☐

☐

☐

☐


25. Simplify the sum. State any restrictions on the variable.

$$\frac{7y+7}{y-3} + \frac{8y+9}{y-3}$$

Select the correct choice below and fill in the answer box(es) to complete your choice.

☐ A. $\frac{7y+7}{y-3} + \frac{8y+9}{y-3} = \underline{\hspace{2cm}}$ for all values of y
(Simplify your answer.)

☐ B. $\frac{7y+7}{y-3} + \frac{8y+9}{y-3} = \underline{\hspace{2cm}}$ for $y \neq \underline{\hspace{2cm}}$
(Simplify your answers. Use a comma to separate answers as needed.)

26. Divide.

$$(x^5 + 32) \div (x + 2)$$

The quotient is $\underline{\hspace{2cm}}$ with a remainder of $\underline{\hspace{2cm}}$.
(Simplify your answers. Use integers or fractions for any numbers in the expression. Do not factor.)

27. Solve the following equation. Check the solution.

$$\frac{16}{p} + \frac{6p-5}{p+2} = 6$$

Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

- ☐ A. The solution is $\underline{\hspace{2cm}}$.
(Type an integer or a simplified fraction. Use a comma to separate answers as needed.)
- ☐ B. There are infinitely many solutions.
- ☐ C. There is no solution.

28. Determine whether the given binomial is a factor of $x^3 + 8x^2 + 7x - 31$.

$$x + 3$$

Is the binomial $x + 3$ a factor of $x^3 + 8x^2 + 7x - 31$?

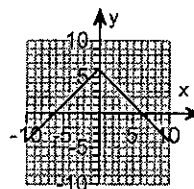
- ☐ No
☐ Yes

- *29. Use transformations of $f(x) = |x|$ to graph the following function.

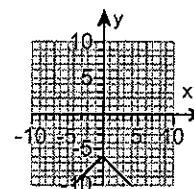
$$h(x) = -|x - 6|$$

Choose the correct graph below.

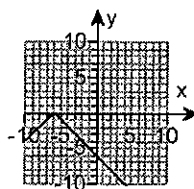
☐ A.



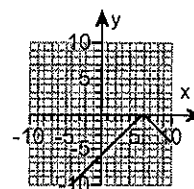
☐ B.



☐ C.



☐ D.



30. Divide using synthetic division.

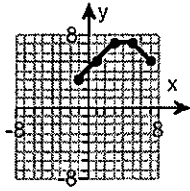
$$\frac{3x^3 + 8x^2 - 9x + 3}{x - 3}$$

$$\frac{3x^3 + 8x^2 - 9x + 3}{x - 3} = \underline{\hspace{2cm}}, \text{ remainder } \underline{\hspace{2cm}}$$

1. B. There is no solution.

2. A. $y =$ -3 (Use a comma to separate answers if needed.)

3.



C.

4. 4

0.1

5. A. $x =$ 3 (Simplify your answer. Use a comma to separate answers as needed.)

6. $\sqrt[5]{x}$

7. A. The product is $\left[\frac{-27}{-36} \quad \frac{-18}{-18} \right]$. (Simplify your answers.)

8. $\sqrt[3]{3^2}$

9. A. The solution is $z =$ -3, -1 . (Use a comma to separate answers as needed.)

10. A. $r =$ 5 (Type an integer or a simplified fraction. Use a comma to separate answers as needed.)

11. $(x - 2)(x + 4)$

12. A. $5C = \left[\frac{10}{10} \quad \frac{-45}{20} \right]$ (Simplify your answers.)

13. A. The solution is $y =$ 6 .

(Type an integer or a simplified fraction. Use a comma to separate answers as needed.)

14. 51.4

15. 7

-2

-3

2

16. $3x + 2$

9

17. 6

18. A.
$$\begin{bmatrix} -8 & 8 & 2 \\ -8 & -8 & -2 \end{bmatrix} \begin{bmatrix} -6 \\ -5 \\ -7 \end{bmatrix} = \begin{bmatrix} -6 \\ 102 \end{bmatrix}$$

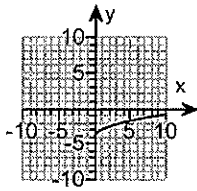
19. 11

30

35

-22

20.



D.

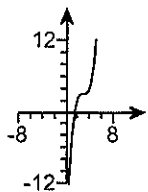
21. $x^{5/4}$

22. 109

23. $x^3 - 2x^2 - 2x + 4$

-34

24.



25. B. $\frac{7y+7}{y-3} + \frac{8y+9}{y-3} = \frac{15y+16}{y-3}$ for $y \neq 3$

(Simplify your answers. Use a comma to separate answers as needed.)

26. $x^4 - 2x^3 + 4x^2 - 8x + 16$

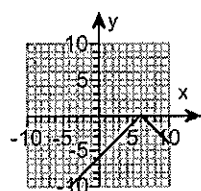
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27. A. The solution is **32**.

(Type an integer or a simplified fraction. Use a comma to separate answers as needed.)

28. No

29.



D.

30. $3x^2 + 17x + 42$

129