# **Unit 01 - Foundations For Algebra**

Content Area: Mathematics
Course(s): Algebra I
Time Period: September
Length: 13 days
Status: Published

### **Enduring Understandings**

- Algebra uses symbols to represent quantities that are unknown or that vary.
- Relationships that are always true for real numbers are called properties, which are rules used to rewrite and compare expressions
- Sometimes the value of one quantity can be found if you know the value of another.
- The rules for multiplying real numbers are related to the properties of real numbers and the definitions of operations.
- You can add or subtract any real numbers using a number line model.
- You can add or subtract real numbers using rules involving absolute value.
- You can approximate the square roots of nonnegative numbers
- You can represent mathematical phrases and real-world relationships using symbols and operations.
- You can represent the relationship between the quantities in different ways, including tables, equations, and graphs.
- You can use an equation to represent the relationship between two quantities that have the same value.
- You can use powers to shorten how you represent repeated multiplication such as 2 x 2 x 2 x 2
- You can use the Distributive Property to simplify the product of a number and a sum or difference

# **Essential Questions**

- How are properties related to algebra?
- How can you represent quantities, patterns, and relationships?
- · What do parenthesis do in an arithmetic expression?
- What procedures can be used to simplify an expression?
- Why does order of operation matter when simplifying?

#### **Lesson Titles**

- Combining Like Terms
- Distributive Property
- Order of Operations
- Signed Numbers
- Solving One Step Equations

### Standards/Indicators

MA.K-12.1

Make sense of problems and persevere in solving them.

Mathematically proficient students start by explaining to themselves the meaning of a problem and looking for entry points to its solution. They analyze givens, constraints, relationships, and goals. They make conjectures about the form and meaning of the solution and plan a solution pathway rather than simply jumping into a solution attempt. They consider analogous problems, and try special cases and simpler forms of the original problem in order to gain insight into its solution. They monitor and evaluate their progress and change course if necessary. Older students might, depending on the context of the problem, transform algebraic expressions or change the viewing window on their graphing calculator to get the information they need. Mathematically proficient students can explain correspondences between equations, verbal descriptions, tables, and graphs or draw diagrams of important features and relationships, graph data, and search for regularity or trends. Younger students might rely on using concrete objects or pictures to help conceptualize and solve a problem. Mathematically proficient students check their answers to problems using a different method, and they continually ask themselves, "Does this make sense?" They can understand the approaches of others to solving complex problems and identify correspondences between different approaches.

MA.A-SSE.A.1

Interpret expressions that represent a quantity in terms of its context.

Reason abstractly and quantitatively.

MA.K-12.2

Mathematically proficient students make sense of quantities and their relationships in problem situations. They bring two complementary abilities to bear on problems involving quantitative relationships: the ability to decontextualize—to abstract a given situation and represent it symbolically and manipulate the representing symbols as if they have a life of their own, without necessarily attending to their referents—and the ability to contextualize, to pause as needed during the manipulation process in order to probe into the referents for the symbols involved. Quantitative reasoning entails habits of creating a coherent representation of the problem at hand; considering the units involved; attending to the meaning of quantities, not just how to compute them; and knowing and flexibly using different properties of operations and objects.

MA.A-SSE.A.1a

Interpret parts of an expression, such as terms, factors, and coefficients.

MA.K-12.3

Construct viable arguments and critique the reasoning of others.

Mathematically proficient students understand and use stated assumptions, definitions, and previously established results in constructing arguments. They make conjectures and build a logical progression of statements to explore the truth of their conjectures. They are able to analyze situations by breaking them into cases, and can recognize and use counterexamples. They justify their conclusions, communicate them to others, and respond to the arguments of others. They reason inductively about data, making plausible arguments that take into account the context from which the data arose. Mathematically proficient students are also able to compare the effectiveness of two plausible arguments, distinguish correct logic or reasoning from that which is flawed, and—if there is a flaw in an argument—explain what it is. Elementary students can construct arguments using concrete referents such as objects, drawings, diagrams, and actions. Such arguments can make sense and be correct, even though they are not generalized or made formal until later grades. Later, students learn to determine domains to which an argument applies. Students at all grades can listen or read the arguments of others, decide whether they make sense, and ask useful questions to clarify or improve the arguments.

MA.K-12.4

Model with mathematics.

MA.N-RN.B.3

Explain why the sum or product of two rational numbers is rational; that the sum of a rational number and an irrational number is irrational; and that the product of a nonzero rational number and an irrational number is irrational.

Mathematically proficient students can apply the mathematics they know to solve

problems arising in everyday life, society, and the workplace. In early grades, this might be as simple as writing an addition equation to describe a situation. In middle grades, a student might apply proportional reasoning to plan a school event or analyze a problem in the community. By high school, a student might use geometry to solve a design problem or use a function to describe how one quantity of interest depends on another. Mathematically proficient students who can apply what they know are comfortable making assumptions and approximations to simplify a complicated situation, realizing that these may need revision later. They are able to identify important quantities in a practical situation and map their relationships using such tools as diagrams, two-way tables, graphs, flowcharts and formulas. They can analyze those relationships mathematically to draw conclusions. They routinely interpret their mathematical results in the context of the situation and reflect on whether the results make sense, possibly improving the model if it has not served its purpose.

MA.K-12.5

Use appropriate tools strategically.

Mathematically proficient students consider the available tools when solving a mathematical problem. These tools might include pencil and paper, concrete models, a ruler, a protractor, a calculator, a spreadsheet, a computer algebra system, a statistical package, or dynamic geometry software. Proficient students are sufficiently familiar with tools appropriate for their grade or course to make sound decisions about when each of these tools might be helpful, recognizing both the insight to be gained and their limitations. For example, mathematically proficient high school students analyze graphs of functions and solutions generated using a graphing calculator. They detect possible errors by strategically using estimation and other mathematical knowledge. When making mathematical models, they know that technology can enable them to visualize the results of varying assumptions, explore consequences, and compare predictions with data. Mathematically proficient students at various grade levels are able to identify relevant external mathematical resources, such as digital content located on a website, and use them to pose or solve problems. They are able to use technological tools to explore and deepen their understanding of concepts.

MA.K-12.6

Attend to precision.

Mathematically proficient students try to communicate precisely to others. They try to use clear definitions in discussion with others and in their own reasoning. They state the meaning of the symbols they choose, including using the equal sign consistently and appropriately. They are careful about specifying units of measure, and labeling axes to clarify the correspondence with quantities in a problem. They calculate accurately and efficiently, express numerical answers with a degree of precision appropriate for the problem context. In the elementary grades, students give carefully formulated explanations to each other. By the time they reach high school they have learned to examine claims and make explicit use of definitions.

MA.K-12.7

MA.K-12.8

Look for and make use of structure.

Mathematically proficient students look closely to discern a pattern or structure. Young students, for example, might notice that three and seven more is the same amount as seven and three more, or they may sort a collection of shapes according to how many sides the shapes have. Later, students will see  $7 \times 8$  equals the well remembered  $7 \times 5 + 7 \times 3$ , in preparation for learning about the distributive property. In the expression  $x^2 + 9x + 14$ , older students can see the 14 as  $2 \times 7$  and the 9 as 2 + 7. They recognize the significance of an existing line in a geometric figure and can use the strategy of drawing an auxiliary line for solving problems. They also can step back for an overview and shift perspective. They can see complicated things, such as some algebraic expressions, as single objects or as being composed of several objects. For example, they can see  $5 - 3(x - y)^2$  as 5 minus a positive number times a square and use that to realize that its value cannot be more than 5 for any real numbers x and y.

Look for and express regularity in repeated reasoning.

Mathematically proficient students notice if calculations are repeated, and look both for

general methods and for shortcuts. Upper elementary students might notice when dividing 25 by 11 that they are repeating the same calculations over and over again, and conclude they have a repeating decimal. By paying attention to the calculation of slope as they repeatedly check whether points are on the line through (1, 2) with slope 3, middle school students might abstract the equation (y-2)/(x-1)=3. Noticing the regularity in the way terms cancel when expanding (x-1)(x+1),  $(x-1)(x^2+x+1)$ , and  $(x-1)(x^3+x^2+x+1)$  might lead them to the general formula for the sum of a geometric series. As they work to solve a problem, mathematically proficient students maintain oversight of the process, while attending to the details. They continually evaluate the reasonableness of their intermediate results.

MA.A-CED.A.1 Create equations and inequalities in one variable and use them to solve problems.

MA.A-CED.A.2 Create equations in two or more variables to represent relationships between quantities;

graph equations on coordinate axes with labels and scales.

MA.A-REI.D.10 Understand that the graph of an equation in two variables is the set of all its solutions

plotted in the coordinate plane, often forming a curve (which could be a line).

### **Inter-Disciplinary Connections**

Business

- Chemistry
- Computers
- Engineering
- English
- Geography
- History
- Physics

### Warm-Up

- PARCC type of question
- SAT question of the day
- · Skill needed to do lesson
- Use What You Know type of question

# **Anticipatory Set**

- 5 Minute Activity Based
- connecting previous lessons
- connecting vocabulary with roots words
- · Discussion including vocab review/recall
- · Video Clip

## Instructional Strategies, Learning Activities, and Levels of Blooms/DOK

- #1- Blooms Knowledge Remember previously learned information
- #2 Blooms Comprehension Demonstrate an understanding of facts
- #3 Blooms Application Apply Knowledge to actual situations
- #4 Blooms Analysis Break down objects or ideas into simpler parts and find evidence to support generalizations
- #5 Blooms Synthesis Compile component ideas into a new whole or propose alternative solutions
- #6 Blooms Evaluation Make and defend judgments based on internal evidence or external criteria
- · review of solving one step equations
- Review of the rules of combining like terms
- review of the rules of order of operations
- Review of the rules of signed numbers
- Review of the rules of the distributive property
- review warm up
- students will work as a team and explain their work
- · Students will work independently on examples

### **Closure**

- · evaluate your understanding of the lesson
- · Pass out of class
- turn to your partner and discuss

#### **Formative Assessment**

- Edmodo assignments
- Guided Review
- homework/classwork
- Mathxlforschool
- Partner Board Presentation
- Pass Out of Class
- Socrative
- teacher observation
- think-pair-share
- Warm up Review
- White Boards

#### **Summative Assessment**

- quiz
- unit test
- warm up quiz

# **Resources & Technology**

- Algebra 1 Book
- class dojo.com
- color pencils
- desmos.com
- Edmodo
- edpuzzle.com
- Google Forms
- graphing calculator
- Learn Zillion
- mathway.com
- mathxlforschool.com
- quizlet.com
- Remind
- smartboard
- socrative
- student whiteboards
- Teacher Generated Worksheets
- video clips